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(*-- QUADRUPOLE version 1.0 ----- September 18, 2006 --*)
(*----- with Wolfram Mathematica 5.0 -----*)
(*----- Author: R. HAJJAR -----*)

(*-- run --*)
(*-- starts the notebook and determines the nature of the sample: --*)
(*-- a single crystal if numberOfGammaAngles is 1, otherwise a powder --*)
run := Module[{QCC, q, amplitude},
   $\omega_0 = 2 \pi * \text{larmorFrequencyMhz};$ 
  dim = IntegerPart[2 quadrupoleSpin + 1];
  ms = Range[quadrupoleSpin, -quadrupoleSpin, -1];
  Iz = DiagonalMatrix[ms]; (* initial state *)
   $\omega_{\text{rot}} = 2 \pi * \text{spinRatekHz} * 10^{-3};$ 
  QCC = 2  $\pi * \text{QCCMHz};$ 
  q = 2 quadrupoleSpin (2 quadrupoleSpin - 1);
   $A = \frac{\sqrt{6}}{2 q} \text{QCC} * \text{DiagonalMatrix}[(3 \text{ms}^2 - \text{quadrupoleSpin} (\text{quadrupoleSpin} + 1)) / 3];$ 
  If[quadrupoleOrder == 2, {
     $\omega_0 = \sqrt{5} (3 + \eta^2) / 10;$ 
     $\text{amplitude} = \frac{-1}{\omega_0} \frac{\text{QCC}^2}{q^2};$ 
     $A_4 = \frac{\text{amplitude}}{2 \sqrt{70}} (18 \text{quadrupoleSpin} (\text{quadrupoleSpin} + 1) - 34 \text{ms}^2 - 5) \text{ms};$ 
     $A_2 = \frac{\text{amplitude}}{2 \sqrt{14}} (8 \text{quadrupoleSpin} (\text{quadrupoleSpin} + 1) - 12 \text{ms}^2 - 3) \text{ms};$ 
     $A_0 = \frac{\text{amplitude}}{\sqrt{5}} (\text{quadrupoleSpin} (\text{quadrupoleSpin} + 1) - 3 \text{ms}^2) \text{ms};$ 
  }];
  If[numberOfGammaAngles == 1, crystal[ $\alpha_{\text{PR}}$ ,  $\beta_{\text{PR}}$ ,  $\gamma_{\text{PR}}$ ],
    powder[powderFile, numberOfGammaAngles]];
];

(*-- radiofreq --*)
(*-- provides the matrix of an RF pulse --*)
radiofreq[ $\omega_{\text{RF}}$ ] := Module[{RF, ymax},
  HRF = Table[0, {dim}, {dim}];
   $\text{RF} = -\pi * \omega_{\text{RF}} * 10^{-3} \sqrt{\text{quadrupoleSpin} (\text{quadrupoleSpin} + 1) - \text{ms} (\text{ms} - 1)};$ 
  ymax = IntegerPart[quadrupoleSpin + 0.5];
  For[y = 1, y  $\leq$  ymax, y++,
    HRF[[y, y + 1]] = HRF[[y + 1, y]] =
      HRF[[dim - y, dim - y + 1]] = HRF[[dim - y + 1, dim - y]] = RF[[y]];
  ];
];

(*-- pulse --*)
(*-- generates an RF pulse --*)
pulse[tau_,  $\omega_{\text{RF}}$ ] := (
  radiofreq[ $\omega_{\text{RF}}$ ];
  nbPulseIncrement = IntegerPart[tau /  $\Delta t$ ];
  If[nbPulseIncrement == 1, pulsevar, pulsefixe];
);

(*-- pulseFunction--*)

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(*-- provides the density matrix describing the spin system --*)
(*-- excited by an RF pulse --*)
pulseFunction[poub_] :=
  Module[{V20, W20, W40, frequency, HQ1, HQ2, Ha, HT, Tp, T, mat, ρ11, ρ22},
    frequency = (poub - 1) * Δt * ωrot;
    V20 = d1C * Cos[frequency] + d2C * Cos[2 frequency]
          + d1S * Sin[frequency] + d2S * Sin[2 frequency];

    HQ1 = V20 * A;    HQ2 = 0;

    If[quadrupoleOrder == 2, {
      W20 = d21C * Cos[frequency] + d22C * Cos[2 frequency]
            + d21S * Sin[frequency] + d22S * Sin[2 frequency];
      W40 = a40
            + d44S * Sin[4 frequency] + d44C * Cos[4 frequency]
            + d43S * Sin[3 frequency] + d43C * Cos[3 frequency]
            + d42S * Sin[2 frequency] + d42C * Cos[2 frequency]
            + d41S * Sin[ frequency] + d41C * Cos[ frequency];

      HQ2 = DiagonalMatrix[A4 * W40 + A2 * W20 - A0 * W0 ];
    }];

    Ha = HRF + HQ1 + HQ2;
    {HT, Tp} = Eigensystem[N[Ha]];    T = Transpose[Tp];
    mat = DiagonalMatrix[Exp[-i * Δt * HT]];
    ρ11 = T.mat.Tp;    ρ22 = T.Conjugate[mat].Tp;    ρ0 = ρ11.ρ0.ρ22;
  ];

(*-- pulsevar, pulse with variable duration--*)
pulsevar := (
  coef4 += 1;
  pulseFunction[coef4];
);

(*-- pulsefixe, pulse with fixed duration --*)
pulsefixe := Module[{pulseDuration},
  For[b = 1, b ≤ nbPulseIncrement, b++, {
    pulseDuration = b + coef4;
    pulseFunction[pulseDuration];
  }];
  coef4 += nbPulseIncrement;
];

(*-- acq0 --*)
(*-- records the first signal amplitude --*)
acq0 := (s[0] = ρ0);

(*-- acq --*)
(*-- records the signal amplitude --*)
acq[z_] := (s[z] = ρ0);

(*-- store --*)
(*-- saves the state of the system and the delay from the beginning --*)
store[sr_] := (
  d[sr] = ρ0;
  indicRotor = coef4;
);

(*-- recall --*)
(*-- provides the state of the system stored previously --*)

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recall[r_] := (
   $\rho_0 = d[r]$ ;
  coef4 = indicRotor;
);
(*-- filterElt --*)
(*-- keeps the density matrix with specific matrix elements --*)
filterElt[elements_] := Module[{ $\rho_6$ , long, elt1, elt2},
   $\rho_6 = \text{Table}[0, \{\text{dim}\}, \{\text{dim}\}]$ ;
  long = Length[elements];
  For [i = 1, i ≤ long, i++, {
    elt1 = elements[[i, 1]];
    elt2 = elements[[i, 2]];
     $\rho_6[[\text{elt1}, \text{elt2}]] = \rho_0[[\text{elt1}, \text{elt2}]]$ ;
  }];
   $\rho_0 = \rho_6$ ;
];
(*-- filterCoh --*)
(*-- keeps the density matrix with specific coherences --*)
filterCoh[coh_] := Module[{ $\rho_6$ , quanta, qq, long, x, elt1, elt2},
   $\rho_6 = \text{Table}[0, \{\text{dim}\}, \{\text{dim}\}]$ ;

  For [i = 1, i ≤ Length[coh], i++, {
    quanta = coh[[i]];
    qq = Abs [quanta];
    long = dim - qq;
    x = Range[1, long];
    For [z = 1, z ≤ long, z++, {
      If [quanta ≥ 0, {elt1 = x[[z]]; elt2 = x[[z]] + qq},
        {elt2 = x[[z]]; elt1 = x[[z]] + qq}];
       $\rho_6[[\text{elt1}, \text{elt2}]] = \rho_0[[\text{elt1}, \text{elt2}]]$ ;
    }];
  }];

   $\rho_0 = \rho_6$ ;
];
(*-- tabgraph --*)
(*-- presents the simulated amplitudes in a table --*)
(*-- and plots the simulated amplitudes versus pulse duration --*)
tabgraph[nom_String] := (
  Print ["*****"];
  For [a = 0, a ≤ np, a++, pas[a] = a Δt];

  tableau = Table[{t, pas[t], NumberForm[h[t], 10]}, {t, 0, np}];
  Print [TableForm[tableau,
    TableHeadings -> {None, {"Rang", "t (μs)", "intensity"}}]];

  Print ["*****"];
  ListPlot [Table[{pas[t], h[t]}, {t, 0, np}],
    PlotJoined → True,
    AxesLabel → {"t (μs)", "Intensity (A.U.)"},
    PlotStyle → {Hue[0.1]},
    TextStyle → {FontFamily → "Times", FontSize → 12}];
  Print ["*****"];

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Clear[excel];
excel[data_List] :=
  Module[ { file1 = OpenWrite[nom] },
    Scan[ (
      WriteString[file1, First[#]];
      Scan[
        WriteString[file1, "\t", #] &,
        Rest[#]
      ];
      WriteString[file1, "\n"]
    ) &,
    data
  ];
excel[tableau];
);
(*-- crystal --*)
(*-- provides the signal amplitude for a single crystal --*)
crystal[ $\alpha$ _d_,  $\beta$ d_,  $\gamma$ d_] := Module[{ $\alpha$ angle,  $\beta$ angle,  $\gamma$ angle, elt11, elt22},
   $\alpha$ angle =  $\alpha$ d *  $\pi$  / 180;    $\beta$ angle =  $\beta$ d *  $\pi$  / 180;    $\gamma$ angle =  $\gamma$ d *  $\pi$  / 180;

  For[i = 0, i  $\leq$  np, i++, h[i] = 0];

  elt11 = detectelt[[1, 1]]; elt22 = detectelt[[1, 2]];

   $\rho_0$  = startOperator; (* initial state *)

  coefv20Rot[ $\alpha$ angle,  $\beta$ angle,  $\gamma$ angle];
  If[quadrupoleOrder == 2, coefwx0Rot[ $\alpha$ angle,  $\beta$ angle,  $\gamma$ angle]];

  coef4 = 0; fsimulation;

  For[i = 0, i  $\leq$  np, i++,
    h[i] = N[Im[s[i][[elt11, elt22]]]] / numberOfGammaAngles];
  ];
(*-- powder --*)
(*-- provides the signal amplitude for a powder sample --*)
powder[rep_, max $\gamma$ _] :=
  Module[{ $\alpha$ angle,  $\beta$ angle,  $\gamma$ angle, proba, elt11, elt22, fileSize, xtalFile},
    For[i = 0, i  $\leq$  np, i++, h[i] = 0];

    elt11 = detectelt[[1, 1]]; elt22 = detectelt[[1, 2]];

    xtalFile = ReadList[rep, {Number, Number, Number}];
    fileSize = Length[xtalFile];
    Print["powderFile: rep", fileSize, "_simp"];

    For[j = 1, j  $\leq$  fileSize, j++, {
      Print[j, "/", fileSize];
       $\alpha$ angle = xtalFile[[j, 1]] *  $\pi$  / 180;
       $\beta$ angle = xtalFile[[j, 2]] *  $\pi$  / 180;
      proba = xtalFile[[j, 3]];
    }
  ];

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For [g = 0, g < maxγ, g++, {
  ρ0 = startOperator; (* initial state *)
  γangle =  $\frac{2 g \pi}{\text{max}\gamma}$ ;
  coefv20Rot[αangle, βangle, γangle];
  If[quadrupoleOrder == 2, coefwx0Rot[αangle, βangle, γangle]];

  coef4 = 0; fsimulation;

  For[k = 0, k ≤ np, k++, h[k] = h[k] + proba * s[k]];
}];

For[i = 0, i ≤ np, i++,
  h[i] = N[Im[h[i][[elt11, elt22]]]] / numberOfGammaAngles];
];

(*-- coefv20Rot --*)
(*-- provides the parameters dxC and dxS of V20 --*)
coefv20Rot[αeuler_, βeuler_, γeuler_] := Module[{a1, a2, b1, b2},
  c2α = Cos[2 αeuler];   s2α = Sin[2 αeuler];
  cβ = Cos[βeuler];     sβ = Sin[βeuler];
  c2β = Cos[2 βeuler];   s2β = Sin[2 βeuler];
  cγ = Cos[γeuler];     sγ = Sin[γeuler];
  c2γ = Cos[2 γeuler];   s2γ = Sin[2 γeuler];
  a1 = -η * s2α * sβ / √3;      b1 = -(-3 + η * c2α) s2β / (2 √3);
  a2 = -η * cβ * s2α / √6;      b2 = -(η * c2α * (3 + c2β) + 6 sβ2) / (4 √6);
  d2S = a2 * c2γ + b2 * s2γ;    d1S = a1 * cγ + b1 * sγ;
  d2C = a2 * s2γ - b2 * c2γ;    d1C = a1 * sγ - b1 * cγ;
];

(*-- coefwx0Rot --*)
(*-- provides the parameters d4xC and d4xS of W40 --*)
(*-- and the parameters d2xC and d2xS of W20 --*)
coefwx0Rot[αeuler_, βeuler_, γeuler_] :=
  Module[{a22, b22, a21, b21, a41, a42, a43, a44, b41, b42, b43, b44},
    c4α = Cos[4 αeuler];
    c2α = Cos[2 αeuler];   s2α = Sin[2 αeuler];

    c4β = Cos[4 βeuler];   s4β = Sin[4 βeuler];
    c2β = Cos[2 βeuler];   s2β = Sin[2 βeuler];
    cβ = Cos[βeuler];     sβ = Sin[βeuler];

    cγ = Cos[γeuler];     sγ = Sin[γeuler];
    c2γ = Cos[2 γeuler];   s2γ = Sin[2 γeuler];
    c3γ = Cos[3 γeuler];   s3γ = Sin[3 γeuler];
    c4γ = Cos[4 γeuler];   s4γ = Sin[4 γeuler];

    a22 = -√2/7 η * cβ * s2α;   b22 = -(η * c2α (3 + c2β) + sβ2 (-3 + η2)) / (2 √14);
    a21 = -(2/√7) η * sβ * s2α;   b21 = (-3 - 2 c2α * η + η2) s2β / (2 √7);
    d22S = a22 * c2γ + b22 * s2γ;   d21S = a21 * cγ + b21 * sγ;
    d22C = a22 * s2γ - b22 * c2γ;   d21C = a21 * sγ - b21 * cγ;
    a40 =

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$$\frac{-\sqrt{7/10}}{2304} ((18 + \eta^2) (9 + 20 c_{2\beta} + 35 c_{4\beta}) + 240 \eta c_{2\alpha} (5 + 7 c_{2\beta}) s_{\beta}^2 + 280 \eta^2 c_{4\alpha} s_{\beta}^4);$$

a41 =  $(\sqrt{5/7} / 72) \eta * s_{2\alpha} * s_{\beta} (15 + 21 c_{2\beta} + 14 \eta * c_{2\alpha} * s_{\beta}^2);$ 
b41 =  $(\sqrt{5/7} / 288) ((-18 - \eta^2 - 12 \eta * c_{2\alpha} + 7 \eta^2 * c_{4\alpha}) s_{2\beta} - 7 (-3 + \eta * c_{2\alpha})^2 s_{4\beta});$ 
a42 =  $-(\sqrt{5/14} / 18) \eta * c_{\beta} * s_{2\alpha} (-9 + 21 c_{2\beta} + 14 \eta * c_{2\alpha} * s_{\beta}^2);$ 
b42 =  $\frac{-1}{72} \sqrt{5/14}$ 
 $(3 \eta * c_{2\alpha} (5 + 4 c_{2\beta} + 7 c_{4\beta}) + (7 \eta^2 * c_{4\alpha} (3 + c_{2\beta}) + (18 + \eta^2) (5 + 7 c_{2\beta})) * s_{\beta}^2);$ 
a43 =  $-(\sqrt{35} / 72) \eta (-3 - 9 c_{2\beta} + \eta * c_{2\alpha} * (5 + 3 * c_{2\beta})) * s_{2\alpha} * s_{\beta};$ 
b43 =  $-(\sqrt{35} / 288) (-18 - \eta^2 - 12 \eta * c_{2\alpha} + 7 \eta^2 * c_{4\alpha} + 2 (-3 + \eta * c_{2\alpha})^2 * c_{2\beta}) s_{2\beta};$ 
a44 =  $-(\sqrt{35/2} / 72) \eta * c_{\beta} * s_{2\alpha} (\eta * c_{2\alpha} * (3 + c_{2\beta}) + 6 s_{\beta}^2);$ 
b44 =  $-\frac{\sqrt{35/2}}{2304} (\eta^2 * c_{4\alpha} (35 + 28 c_{2\beta} + c_{4\beta}) + 48 \eta * c_{2\alpha} (3 + c_{2\beta}) s_{\beta}^2 + 8 (18 + \eta^2) s_{\beta}^4);$ 
d41S = a41 * cγ + b41 * sγ; d41C = a41 * sγ - b41 * cγ;
d42S = a42 * c2γ + b42 * s2γ; d42C = a42 * s2γ - b42 * c2γ;
d43S = a43 * c3γ + b43 * s3γ; d43C = a43 * s3γ - b43 * c3γ;
d44S = a44 * c4γ + b44 * s4γ; d44C = a44 * s4γ - b44 * c4γ;
];
(* Save these functions in a notebook called QUADRUPOLE *)
Save["QUADRUPOLE", run, radiofreq, pulse, pulseFunction,
pulsevar, pulsefixe, acq0, acq, store, recall, filterElt,
filterCoh, tabgraph, crystal, powder, coefv20Rot, coefwx0Rot];

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