

HIGH-RESOLUTION SOLID-STATE NMR OF QUADRUPOLEAR NUCLEI

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[HTTP://WWW.GRANDINETTI.ORG](http://www.grandinetti.org)

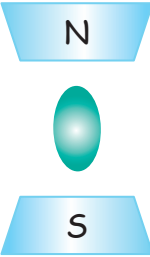
**TUTORIAL LECTURE PRESENTED AT THE
BRUKER USER'S MEETING
BRECKENRIDGE, COLORADO
JULY 2007**

THE BIG PICTURE

ALLOWED NUCLEAR MULTIPOLE MOMENTS AS A FUNCTION OF SPIN I

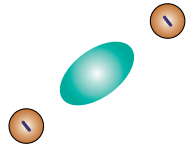
	$l = 0$	$l = 1$	$l = 2$	$l = 3$	$l = 4$
SPIN	monopole	dipole	quadrupole	octapole	hexadecapole
$I = 0$	electric	0	0	0	0
$I = \frac{1}{2}$	electric	magnetic	0	0	0
$I = 1$	electric	magnetic	electric	0	0
$I = \frac{3}{2}$	electric	magnetic	electric	magnetic	0
$I = 2$	electric	magnetic	electric	magnetic	electric

NUCLEAR MAGNETIC
DIPOLE MOMENT COUPLES
TO MAGNETIC FIELD



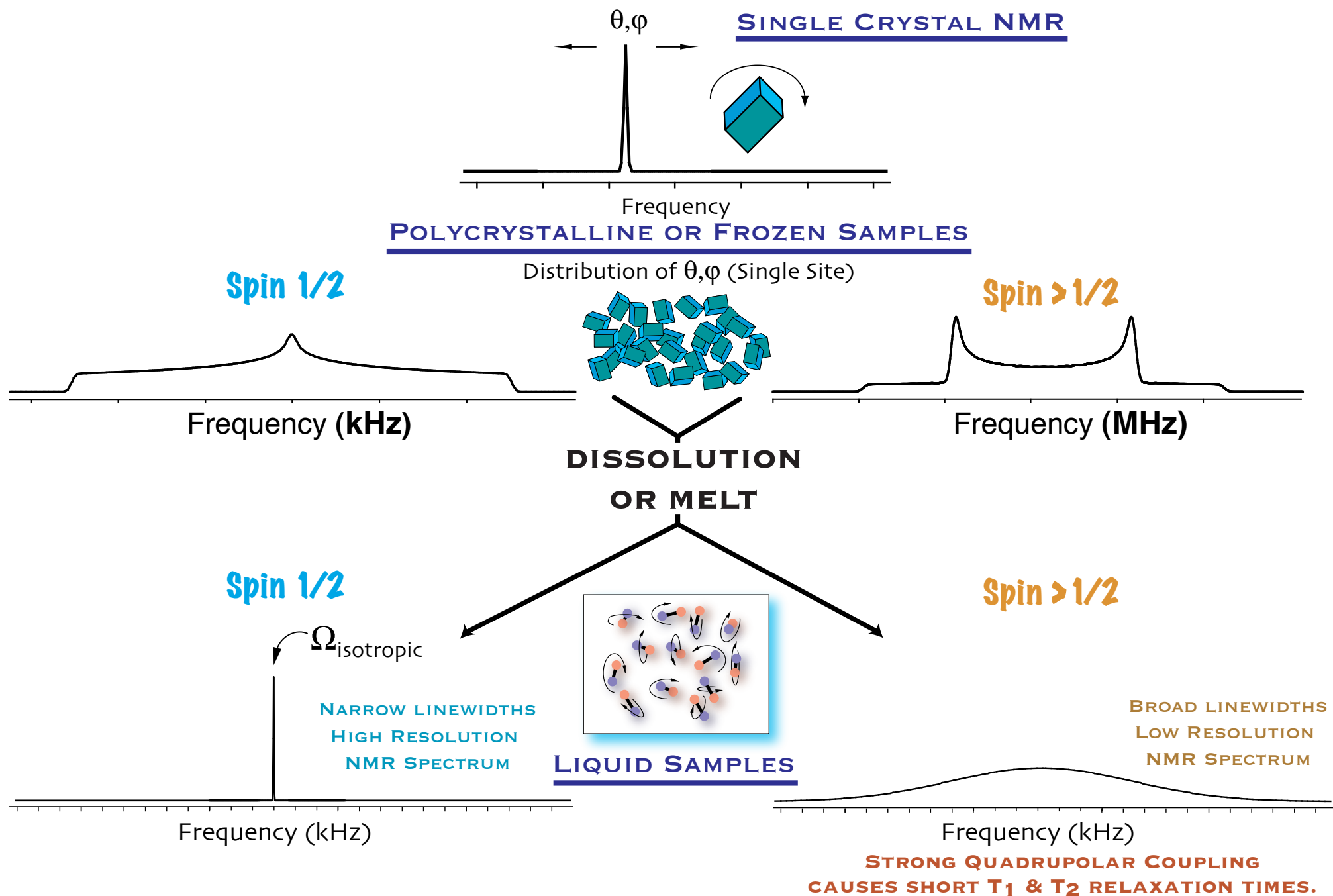
IA																	VIIIA	
H	IIA		Spin = 1/2										Spin > 1/2		He			
Li	Be											B	C	N	O	F	Ne	
Na	Mg	IIIB	IVB	VB	VIB	VIIIB	VIII B				IB	IIB	Al	Si	P	S	Cl	Ar
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr	
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe	
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn	
Fr	Rd	Ac																
		Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu			
		Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr			

NUCLEAR ELECTRIC
QUADRUPOLE MOMENT
COUPLES TO ELECTRIC
FIELD GRADIENT



NMR OF QUADRUPOLEAR NUCLEI

IS THERE A PROBLEM?



PERTURBATION EXPANSION OF NMR TRANSITION FREQUENCY

$$\Omega(\theta, \phi) = \underbrace{\Omega^{(0)}}_{\text{ZEEMAN COUPLING}} + \underbrace{\Omega^{(1)}(\theta, \phi)}_{\text{CHEMICAL SHIFT J-COUPLING DIPOLAR COUPLING QUADRUPOLAR COUPLING}} + \underbrace{\Omega^{(2)}(\theta, \phi) + \Omega^{(3)}(\theta, \phi) + \dots}_{\text{QUADRUPOLAR COUPLING}}$$

ZERO-ORDER
 $\Omega^{(0)} = \omega_0 = -\gamma B_0$
(0 TO HUNDREDS OF MHZ)

FIRST-ORDER CORRECTION

$$\Omega^{(1)}(\theta, \phi) = \Omega_{iso}^{(1)}(I, m_i, m_f) + \sum_{k=-2}^2 c_{2,k}^{(1)}(I, m_i, m_f) Y_{2,k}(\theta, \phi)$$

ω_q **(0 TO TENS OF MHZ)**

$$\omega_q = \frac{6\pi C_q}{2I(2I - 1)}$$

SECOND-ORDER CORRECTION

$$\Omega^{(2)}(\theta, \phi) = \Omega_{iso}^{(2)}(I, m_i, m_f) + \sum_{k=-2}^2 c_{2,k}^{(2)}(I, m_i, m_f) Y_{2,k}(\theta, \phi) + \sum_{k=-4}^4 c_{4,k}^{(2)}(I, m_i, m_f) Y_{4,k}(\theta, \phi)$$

ω_q^2 / ω_0 **(0 TO HUNDREDS OF KHZ)**

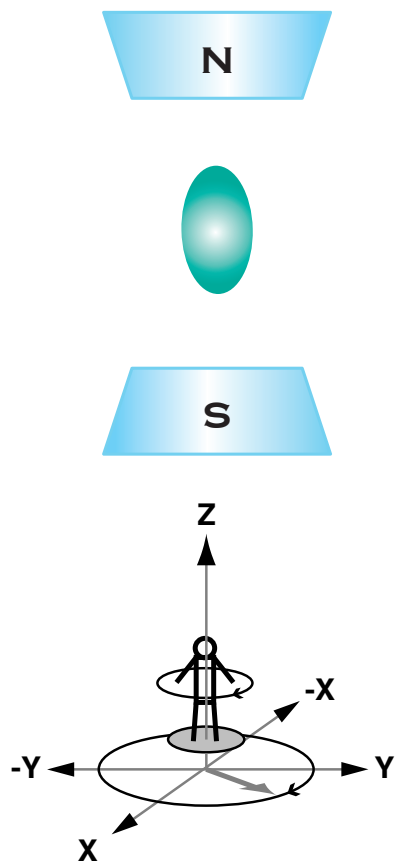
THIRD-ORDER CORRECTION

$$\Omega^{(3)}(\theta, \phi) = \Omega_{iso}^{(3)}(I, m_i, m_f) + \sum_{k=-2}^2 c_{2,k}^{(3)}(I, m_i, m_f) Y_{2,k}(\theta, \phi) + \sum_{k=-4}^4 c_{4,k}^{(3)}(I, m_i, m_f) Y_{4,k}(\theta, \phi) + \sum_{k=-6}^6 c_{6,k}^{(3)}(I, m_i, m_f) Y_{6,k}(\theta, \phi)$$

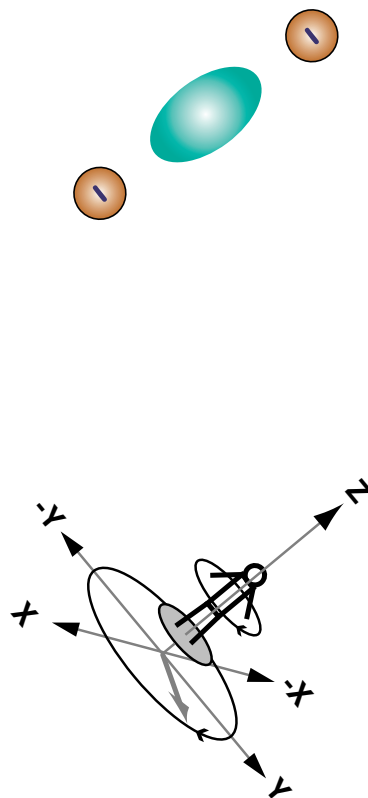
ω_q^3 / ω_0^2 **(0 TO HUNDREDS OF HZ)**

HIGHER ORDER EFFECTS OF QUADRUPOLEAR NUCLEI ON NMR

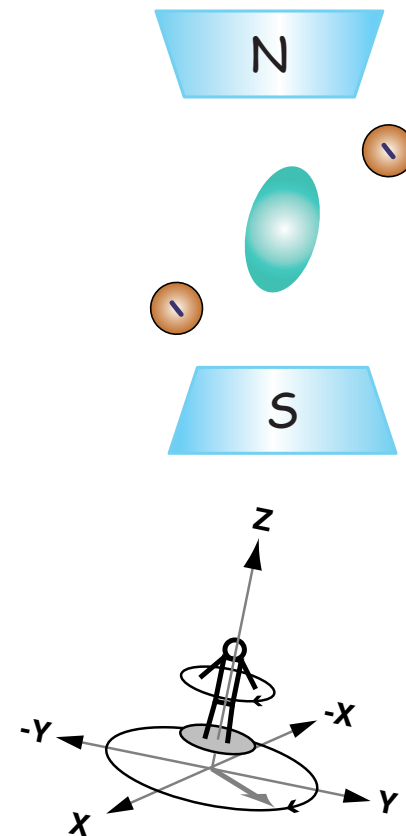
NUCLEAR MAGNETIC DIPOLE MOMENT COUPLES TO MAGNETIC FIELD



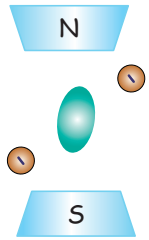
NUCLEAR ELECTRIC QUADRUPOLE MOMENT COUPLES TO ELECTRIC FIELD GRADIENT



=



M → -M TRANSITIONS ARE UNAFFECTED BY FIRST-ORDER QUADRUPOLEAR SPLITTING



ZEEMAN

0TH

QUADRUPOLEAR INTERACTION

1ST

2ND

3RD

<p>SINGLE QUANTUM TRANSITIONS</p>	$\Omega_{ST_-}(\theta, \phi) = \Omega^{(0)} + \Omega_{ST_-}^{(1)}(\theta, \phi) + \Omega_{ST}^{(2)}(\theta, \phi) + \Omega_{ST_-}^{(3)}(\theta, \phi) + \dots$ $\Omega_{CT}(\theta, \phi) = \Omega^{(0)} + 0 + \Omega_{CT}^{(2)}(\theta, \phi) + 0 + \dots$ $\Omega_{ST_+}(\theta, \phi) = \Omega^{(0)} + \Omega_{ST_+}^{(1)}(\theta, \phi) + \Omega_{ST}^{(2)}(\theta, \phi) + \Omega_{ST_+}^{(3)}(\theta, \phi) + \dots$				
<p>DOUBLE QUANTUM TRANSITIONS</p>	$\Omega_{2Q_-}(\theta, \phi) = 2\Omega^{(0)} + \Omega_{2Q_-}^{(1)}(\theta, \phi) + \Omega_{2Q_-}^{(2)}(\theta, \phi) + \Omega_{2Q_-}^{(3)}(\theta, \phi) + \dots$ $\Omega_{2Q_+}(\theta, \phi) = 2\Omega^{(0)} + \Omega_{2Q_+}^{(1)}(\theta, \phi) + \Omega_{2Q_+}^{(2)}(\theta, \phi) + \Omega_{2Q_+}^{(3)}(\theta, \phi) + \dots$				
<p>TRIPLE QUANTUM TRANSITIONS</p>	$\Omega_{3Q}(\theta, \phi) = 3\Omega^{(0)} + 0 + \Omega_{3Q}^{(2)}(\theta, \phi) + 0 + \dots$				

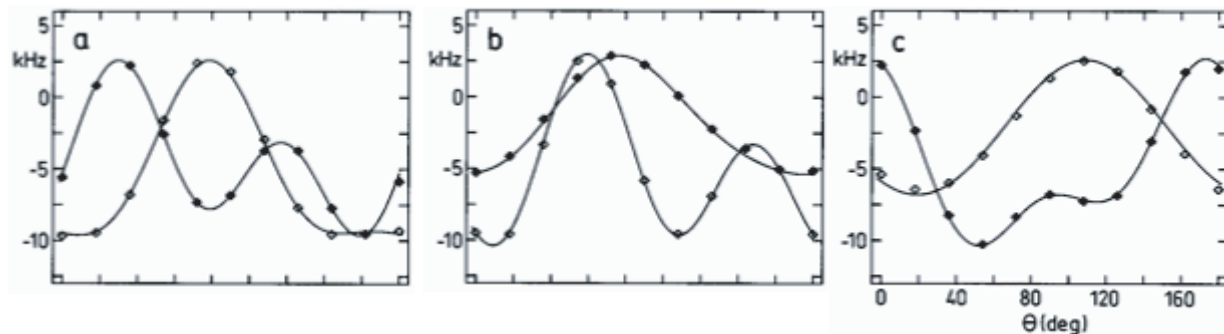
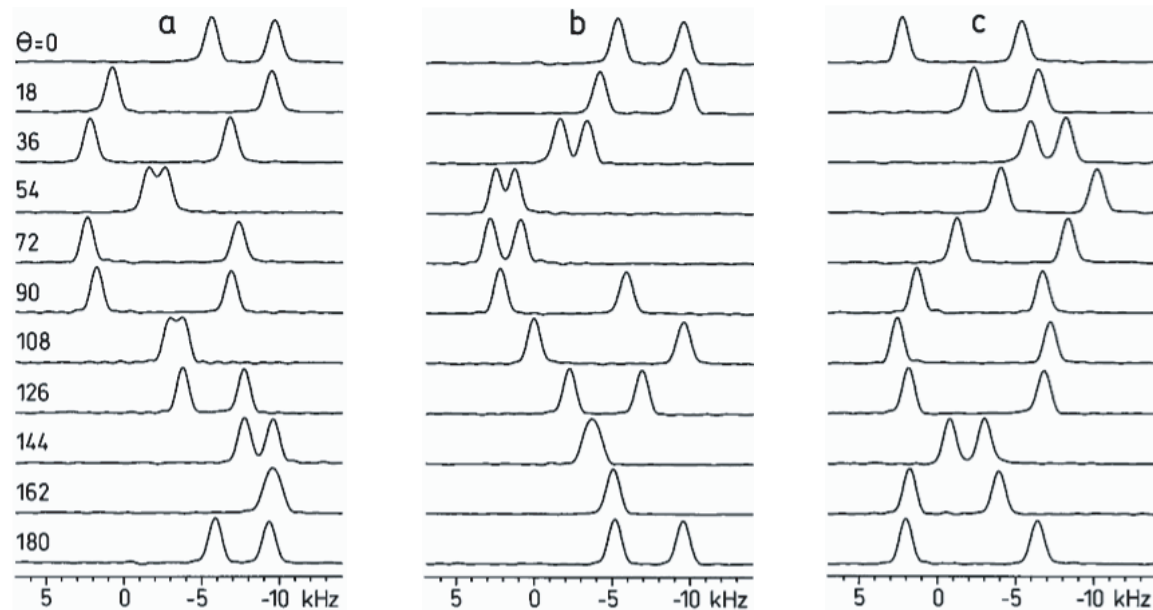
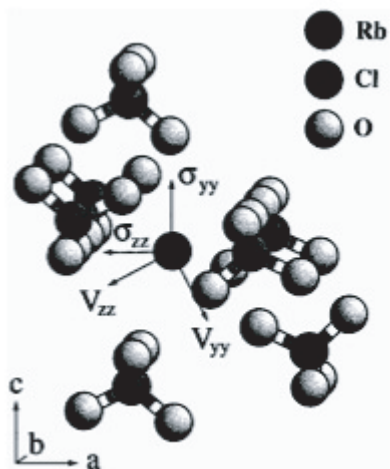
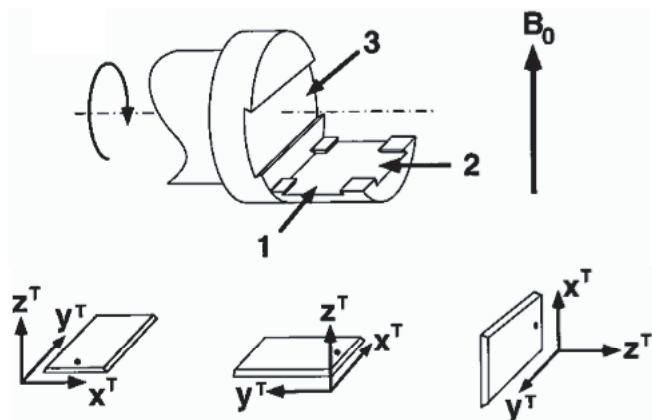
SINGLE CRYSTAL (AND GONIOMETER PROBE)



AVAILABLE?

VOSEGAARD, SKIBSTED, BILDSØE, AND JAKOBSEN, *J. Magn. Reson. A*, **122**, 111-119(1996)

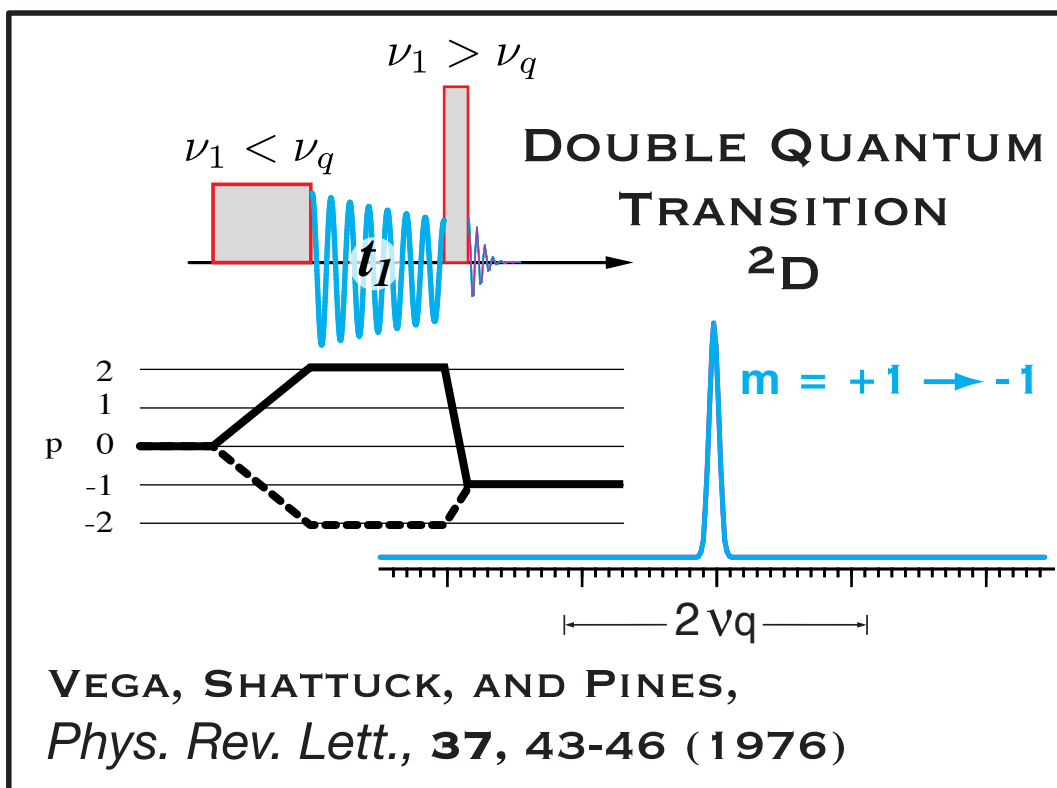
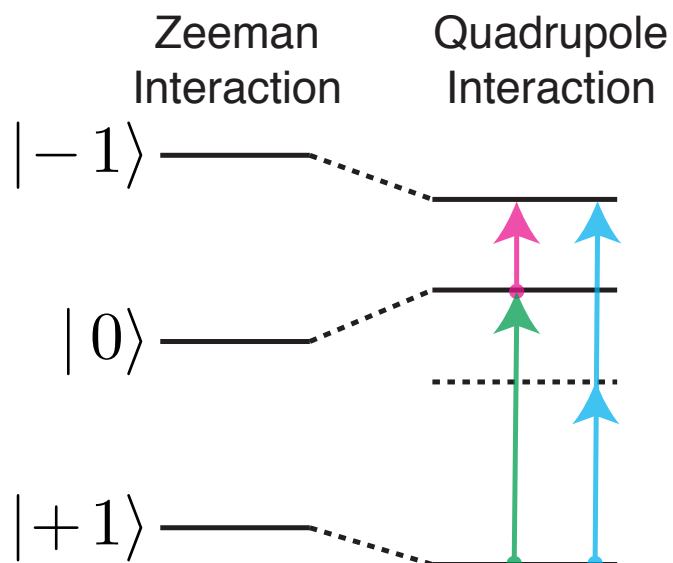
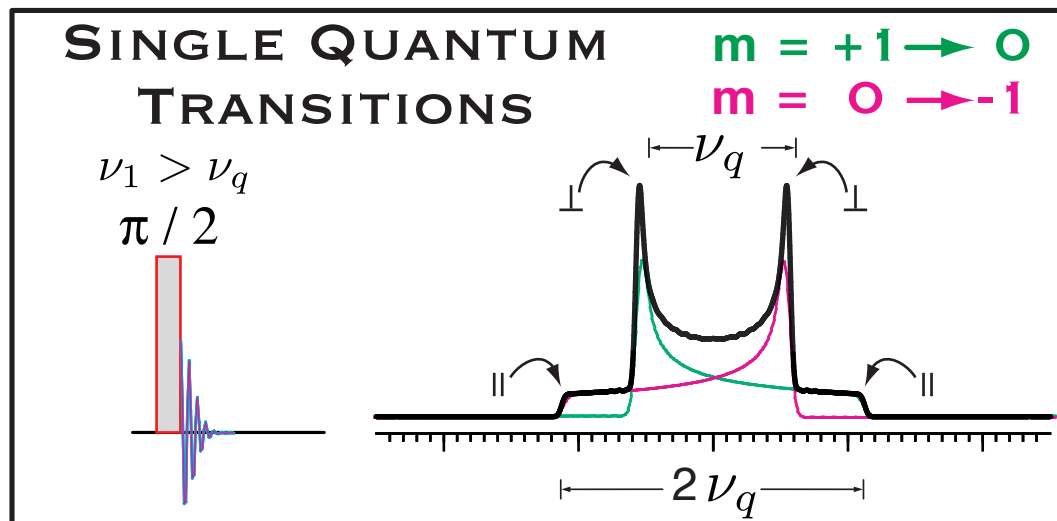
SINGLE CRYSTAL ^{87}Rb NMR OF RbClO_4



Crystal	Site	Method	C_Q (MHz)	η_Q	δ_σ (ppm)	η_σ	δ_{iso} (ppm) ^a	ψ (degree)	χ (degree)	ξ (degree)	Reference
RbClO_4	—	Single-crystal	3.30 ± 0.04	0.21 ± 0.03	13.8 ± 1.5^b	0.61 ± 0.24^b	-13.7 ± 0.6^b	94 ± 14	28 ± 4	87 ± 5	This work
		MAS	3.29 ± 0.05	0.20 ± 0.03	13.5 ± 1.0	0.32 ± 0.20	-13.1 ± 0.3	98 ± 15	34 ± 5	69 ± 20	(7)
		Static	3.24 ± 0.06	0.19 ± 0.06	14 ± 2	0.5 ± 0.3	-14.3 ± 1.8	112 ± 6^c	28.8 ± 1.5^c	16 ± 4^c	(3)

POLYCRYSTALLINE SAMPLES

INTEGER SPINS $^2\text{D}(I=1)$, $^{14}\text{N}(I=1)$, $^{10}\text{B}(I=3)$, $^6\text{Li}(I=1)$



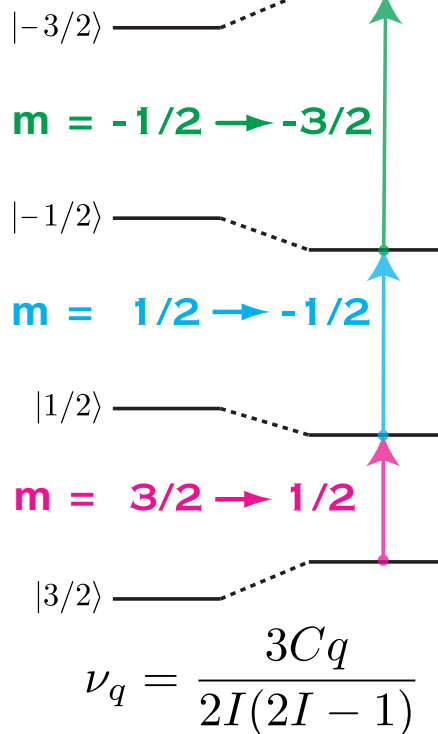
VEGA, SHATTUCK, AND PINES,
Phys. Rev. Lett., **37**, 43-46 (1976)

HALF-INTEGER SPINS: NARROW CENTRAL TRANSITION, BUT MAS IS INADEQUATE

^{87}Rb
 $C_q = 3.2 \text{ MHz}$
 $\eta_q = 0.2$
 $B_0 = 9.4$
 $\nu_0 = 131.45 \text{ MHz}$

Static
 Polycrystalline
 Sample

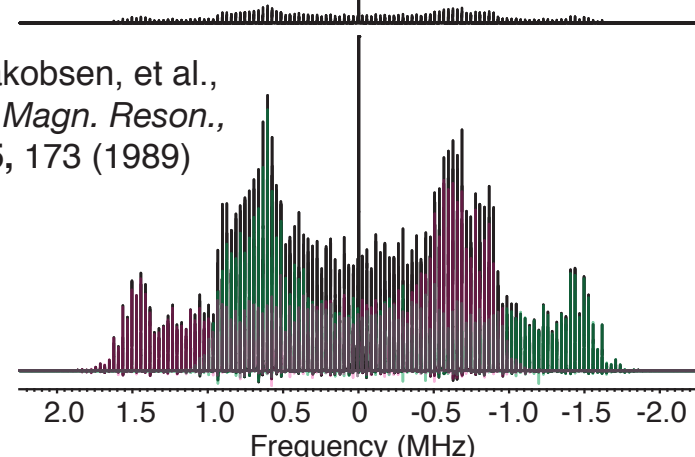
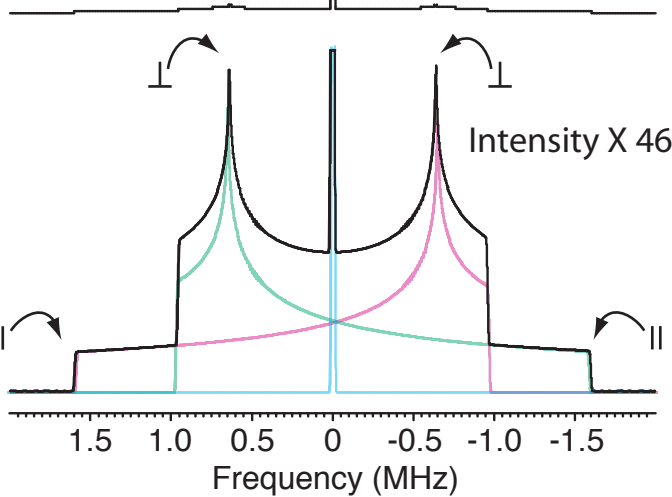
Zeeman Interaction Quadrupole Interaction



Magic-Angle
 Spinning

^{87}Rb
 $C_q = 3.2 \text{ MHz}$
 $\eta_q = 0.2$
 $B_0 = 9.4$
 $\nu_0 = 131.45 \text{ MHz}$
 $\nu_R = 30 \text{ kHz}$

Jakobsen, et al.,
J. Magn. Reson.,
 85, 173 (1989)

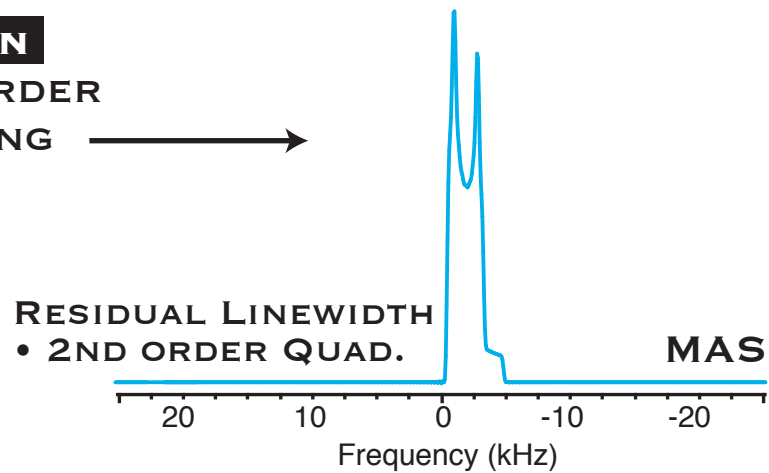
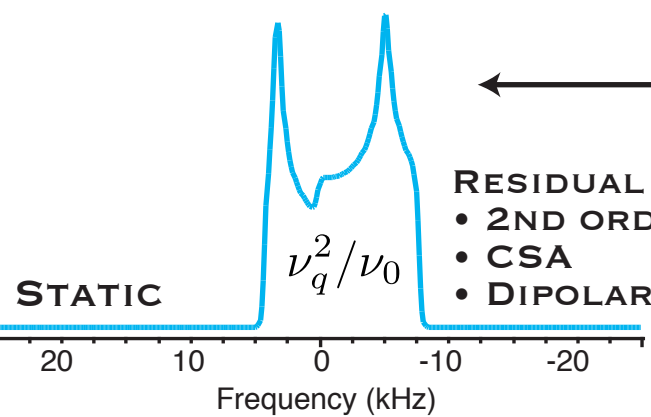


CENTRAL TRANSITION

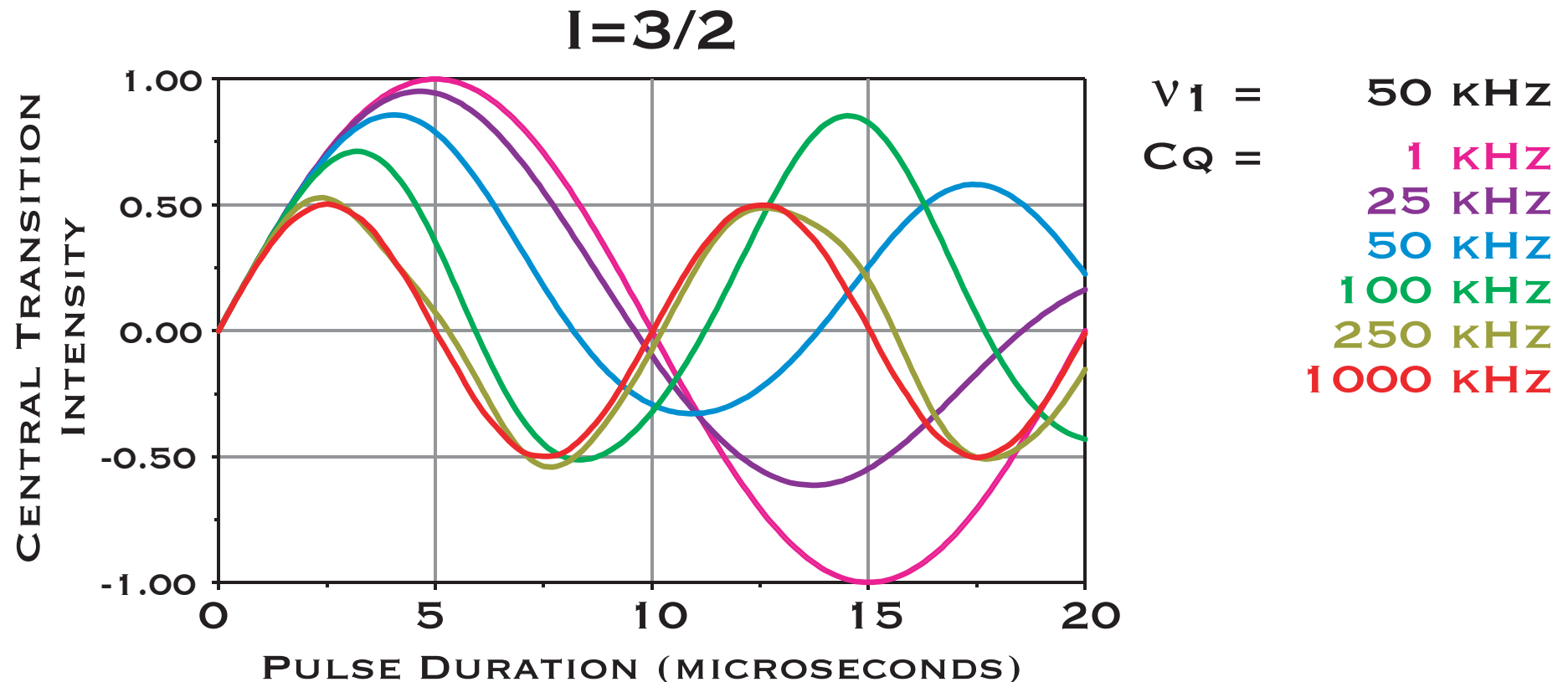
UNAFFECTED BY FIRST ORDER

QUADRUPOLEAR SPLITTING

$m = 1/2 \rightarrow -1/2$



CENTRAL TRANSITION NUTATION FREQUENCY



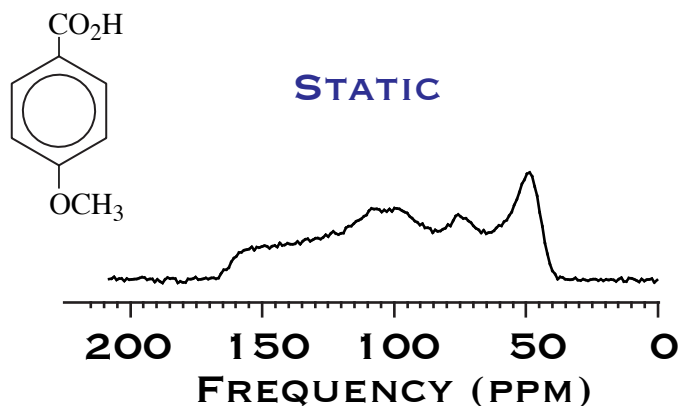
IN THE LIMIT THAT $\omega_1 \ll \omega_q$ THE EFFECTIVE CENTRAL
TRANSITION NUTATION FREQUENCY BECOMES ...

$$(I + 1/2) \omega_1$$

MAGIC-ANGLE SPINNING: GREAT FOR SPIN 1/2, BUT FOR SPIN > 1/2?

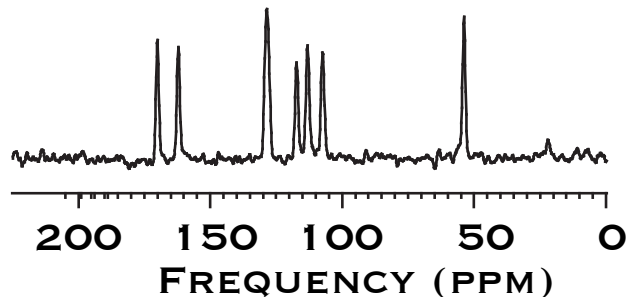
SPIN 1/2

^{13}C NMR SPECTRUM
OF P-ANISIC ACID



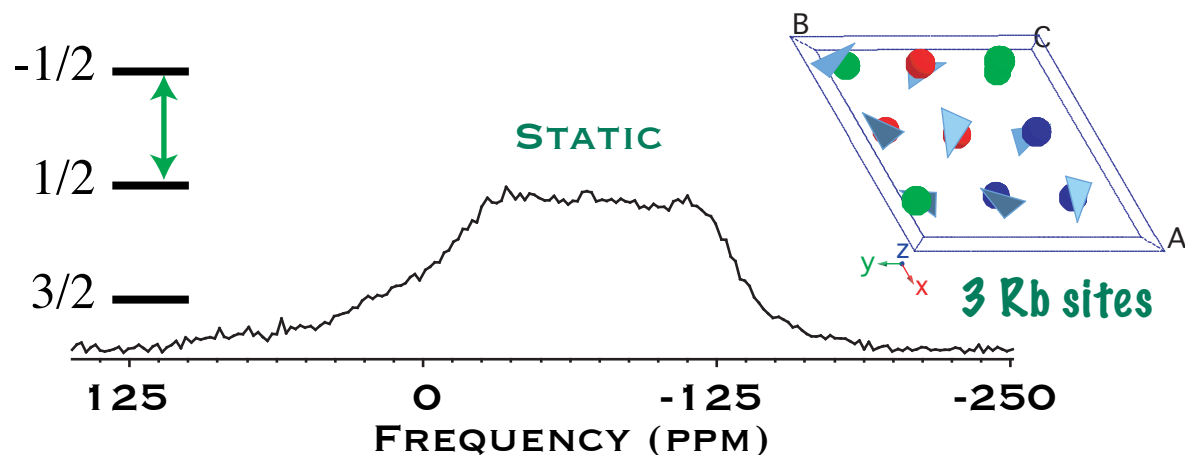
MAS

NARROW LINEWIDTHS
HIGH RESOLUTION



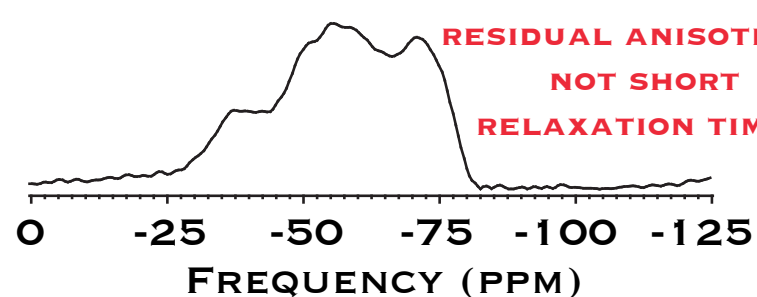
SPIN 3/2

^{87}Rb NMR CENTRAL TRANSITION
SPECTRUM OF RbNO_3



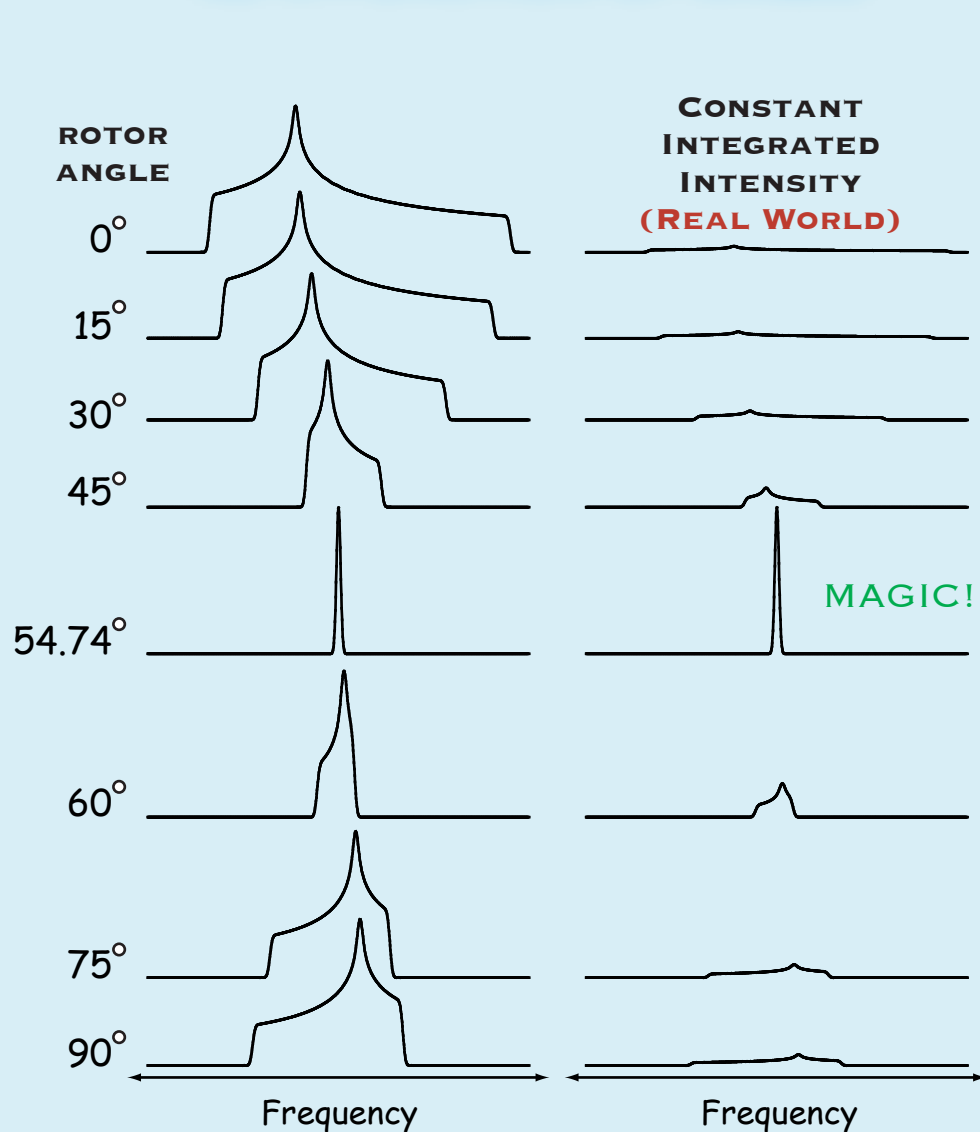
MAS

BROAD LINEWIDTHS
LOW RESOLUTION FROM
RESIDUAL ANISOTROPY,
NOT SHORT
RELAXATION TIMES!

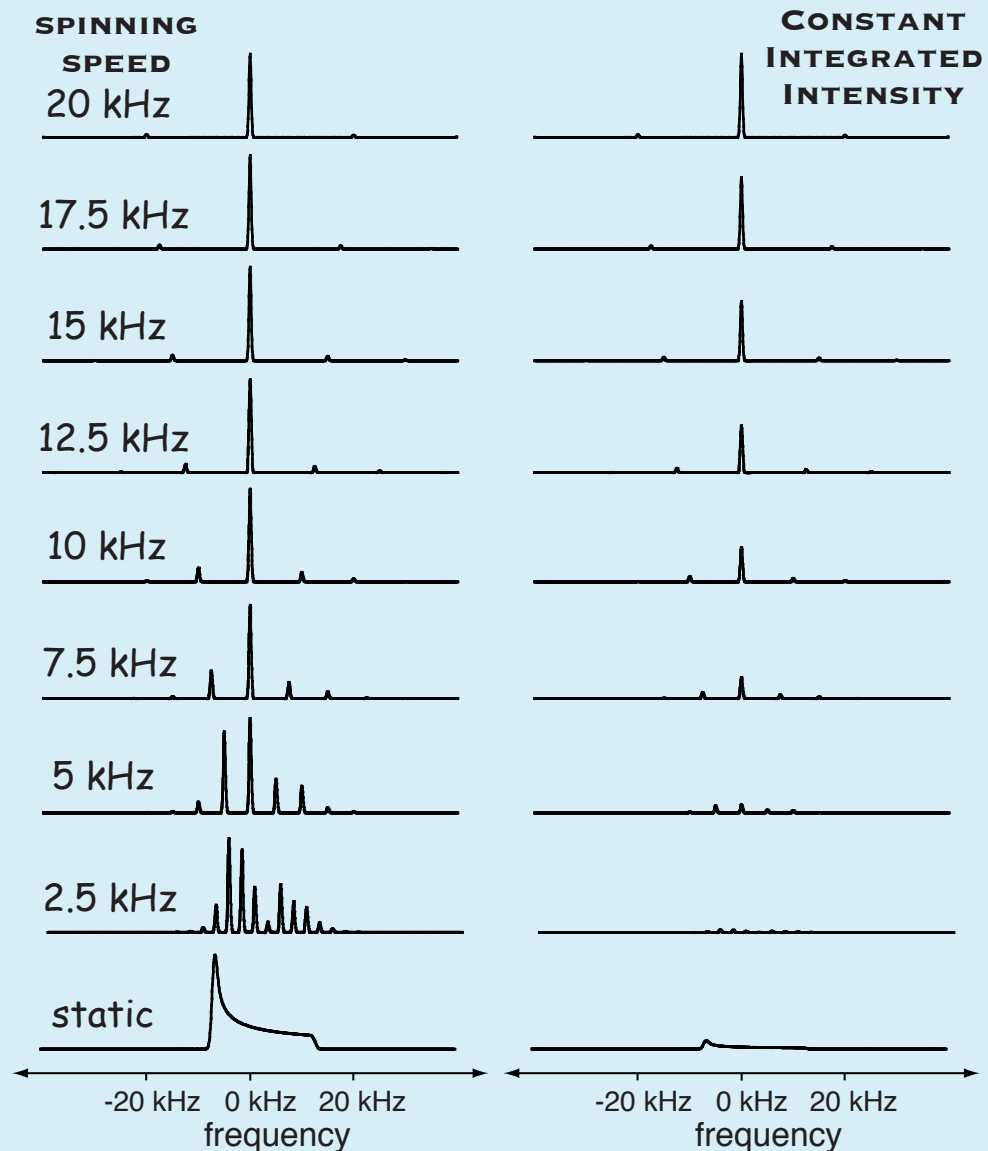


VARIABLE ANGLE SPINNING: SPIN 1/2 NUCLEI

VARIABLE-ANGLE SPINNING SPECTRA AS A FUNCTION OF ANGLE

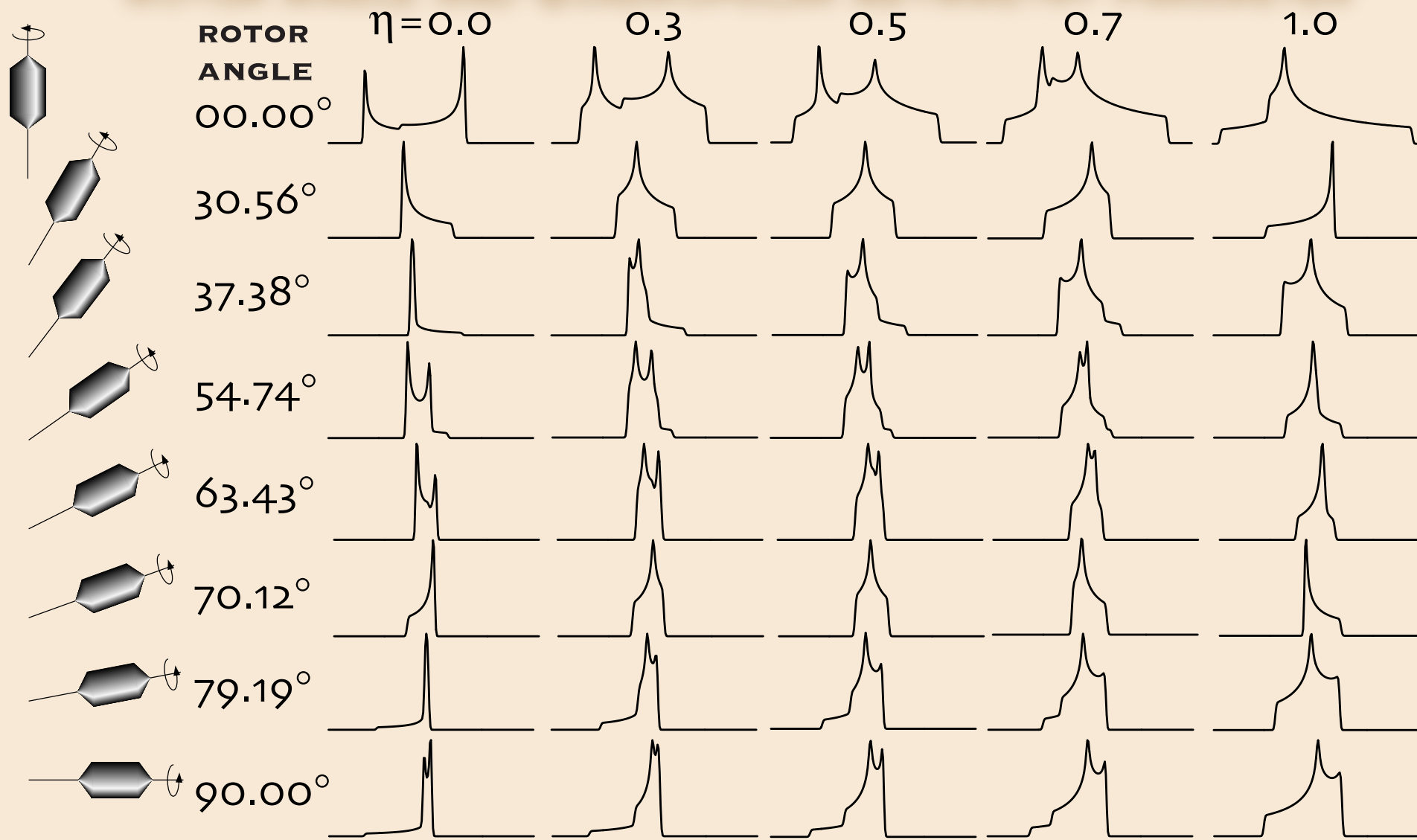


MAGIC-ANGLE SPINNING SPECTRA AS A FUNCTION OF SPINNING SPEED



VARIABLE ANGLE SPINNING: SPIN > 1/2 (QUADRUPOLEAR) NUCLEI

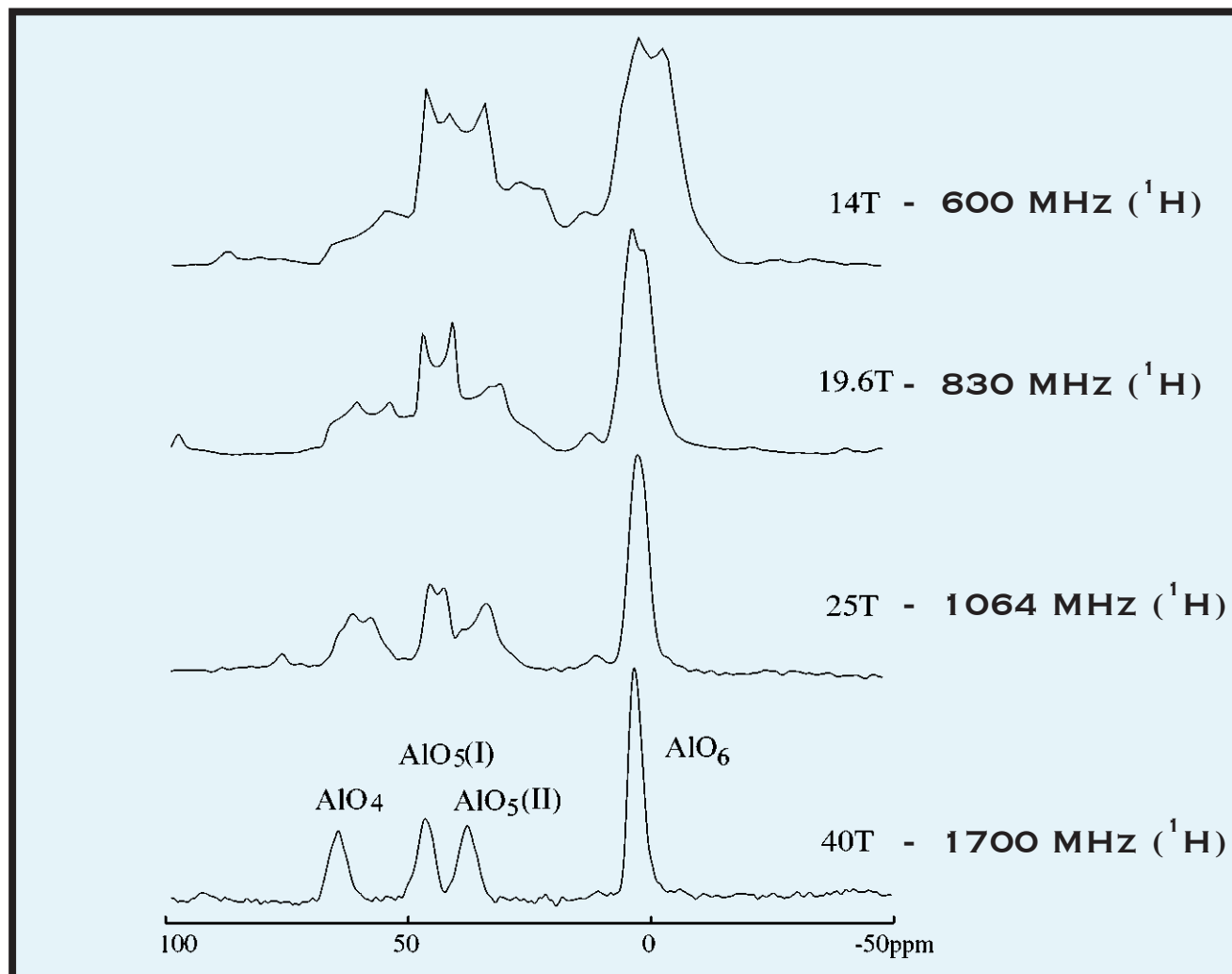
VARIABLE-ANGLE SPINNING AS A FUNCTION OF
ROTOR ANGLE AND QUADRUPOLEAR ASYMMETRY PARAMETER



ONE SOLUTION: REALLY HIGH MAGNETIC FIELDS

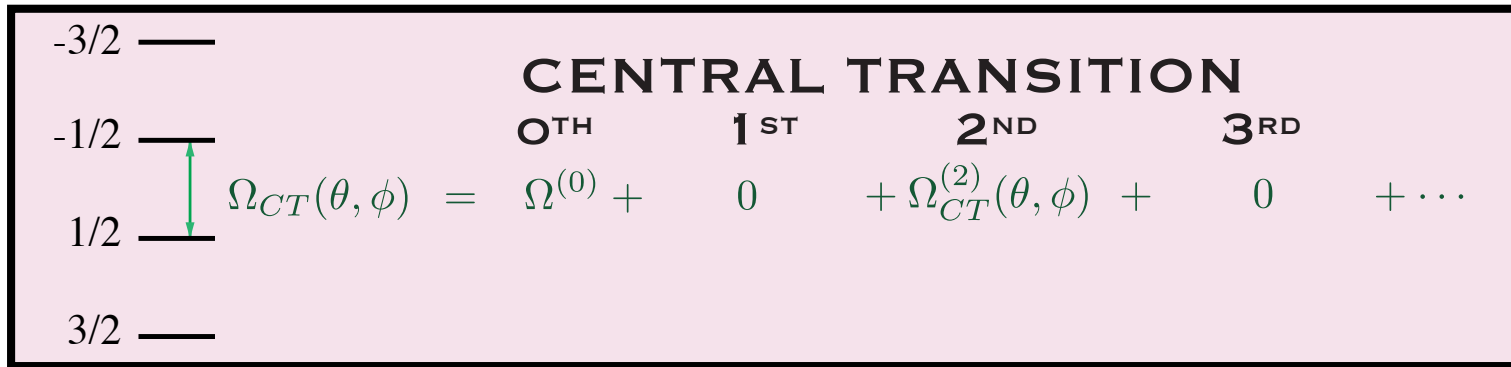
**2ND-ORDER BROADENINGS ARE INVERSELY
PROPORTIONAL TO MAGNETIC FIELD STRENGTH**

^{27}Al MAS spectra of aluminoborate $9\text{Al}_2\text{O}_3 + 2\text{B}_2\text{O}_3$ (A_9B_2) compound from 14 to 40 T.



ANOTHER SOLUTION: BE CLEVER

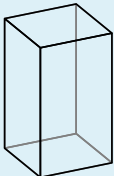
AVERAGING ANISOTROPY OF RANK ℓ



$$\Omega^{(2)}(\theta, \phi) = \Omega_{iso}^{(2)}(I, m_i, m_f) + \sum_{k=-2}^2 c_{2,k}^{(2)}(I, m_i, m_f) Y_{2,k}(\theta, \phi) + \sum_{k=-4}^4 c_{4,k}^{(2)}(I, m_i, m_f) Y_{4,k}(\theta, \phi)$$

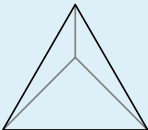
Symmetry

Tetragonal (D₄)



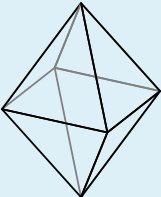
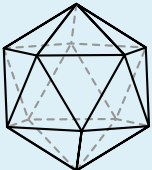
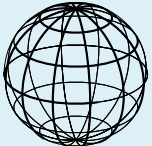
$\ell =$ [0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10]

Tetrahedral (T)



$\ell =$ [0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10]

$\ell \langle A_{\ell,m} \rangle = 0$

Octahedral (O) MAS

$\ell =$ [0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10]

Icosahedral (I)

$\ell =$ [0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10]

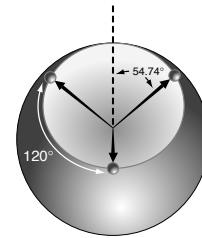
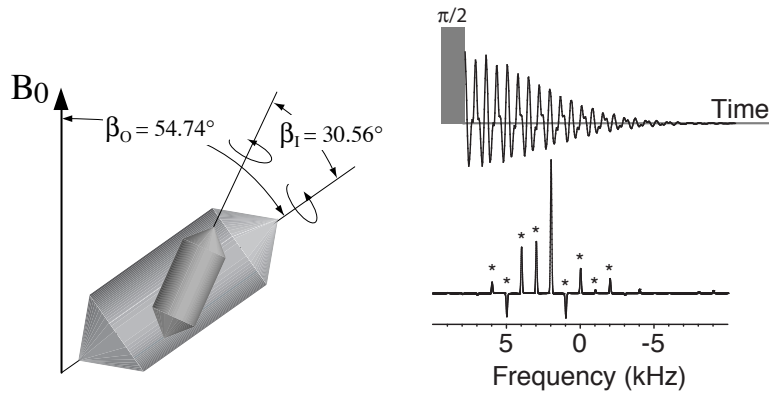
Rotation (SO(3))

$\ell =$ [0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10]

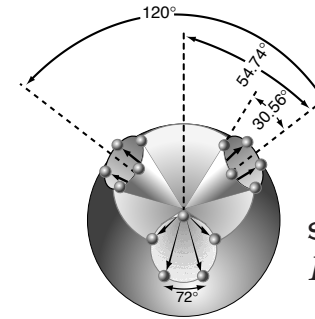
Averaging of spherical harmonics under selected proper point groups and SO(3). (Adapted by permission of Clarendon Press from A. Samoson, B. Q. Sun, and A. Pines, in *Pulsed Magnetic Resonance: NMR, ESR, and Optics - A recognition of E. L. Hahn.*)

A SOLUTION: DOUBLE ROTATION

SAMOSON, LIPPMAN, PINES, MOL. PHYS., 65, 1023(1988).



MAS SYMMETRY



DOR SYMMETRY

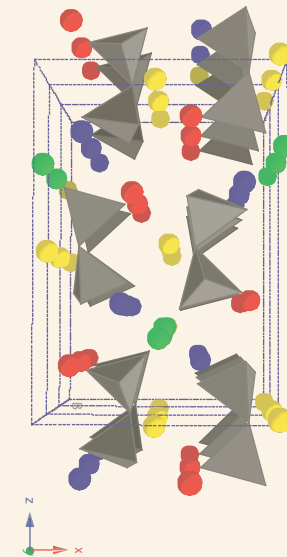
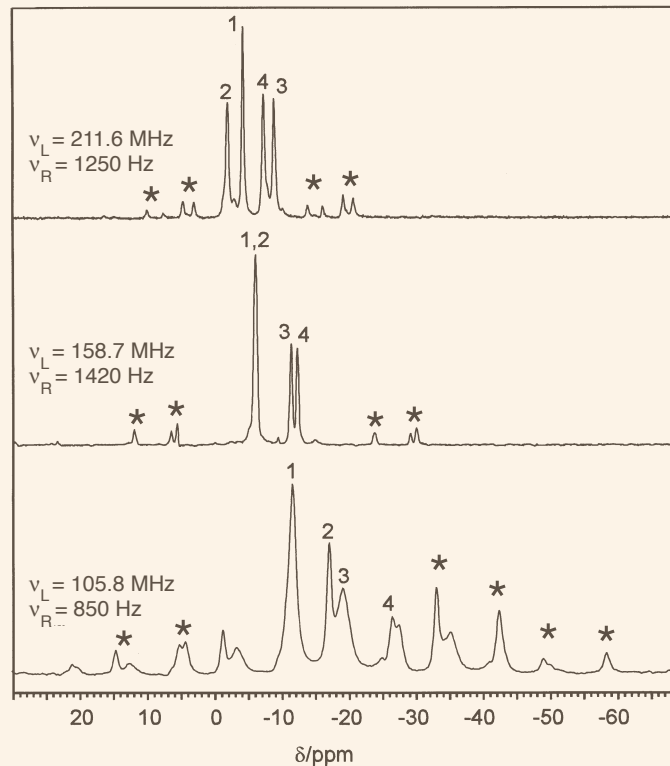
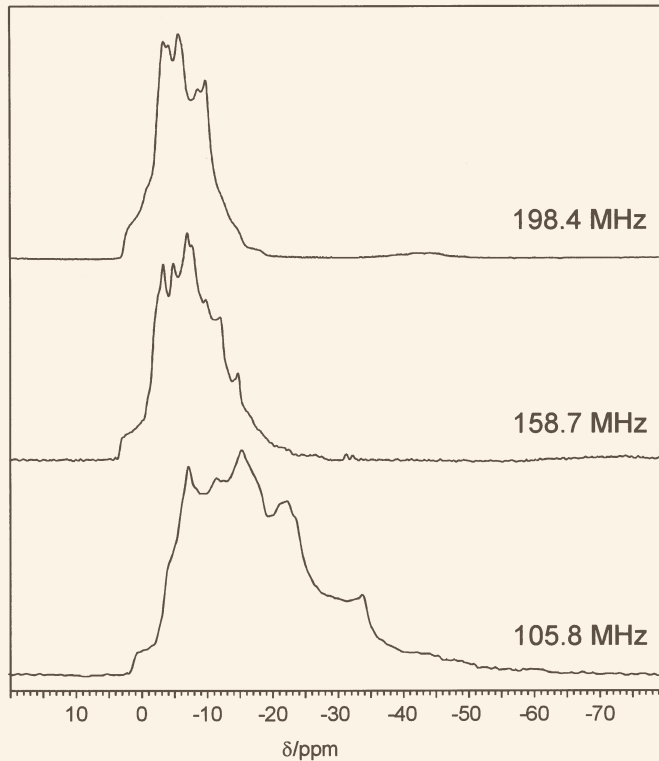
SAMOSON, SUN, AND PINES,
*Pulsed Magnetic Resonance:
NMR, ESR, and Optics*

^{23}Na DOR OF $\text{Na}_4\text{P}_2\text{O}_7$

Engelhardt, Kentgens, Koller, Samoson
Solid State Nuclear Magnetic Resonance 15 1999 171-180

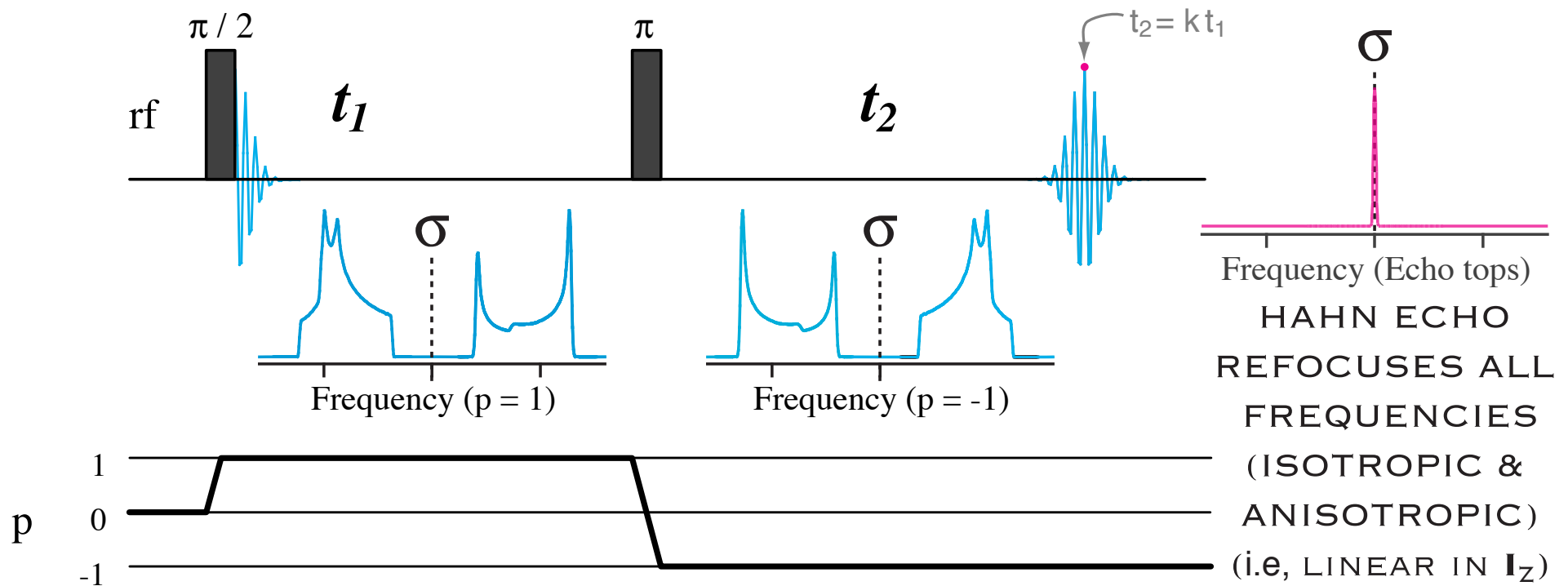
MAGIC ANGLE SPINNING

DOUBLE ROTATION



OTHER SOLUTIONS?

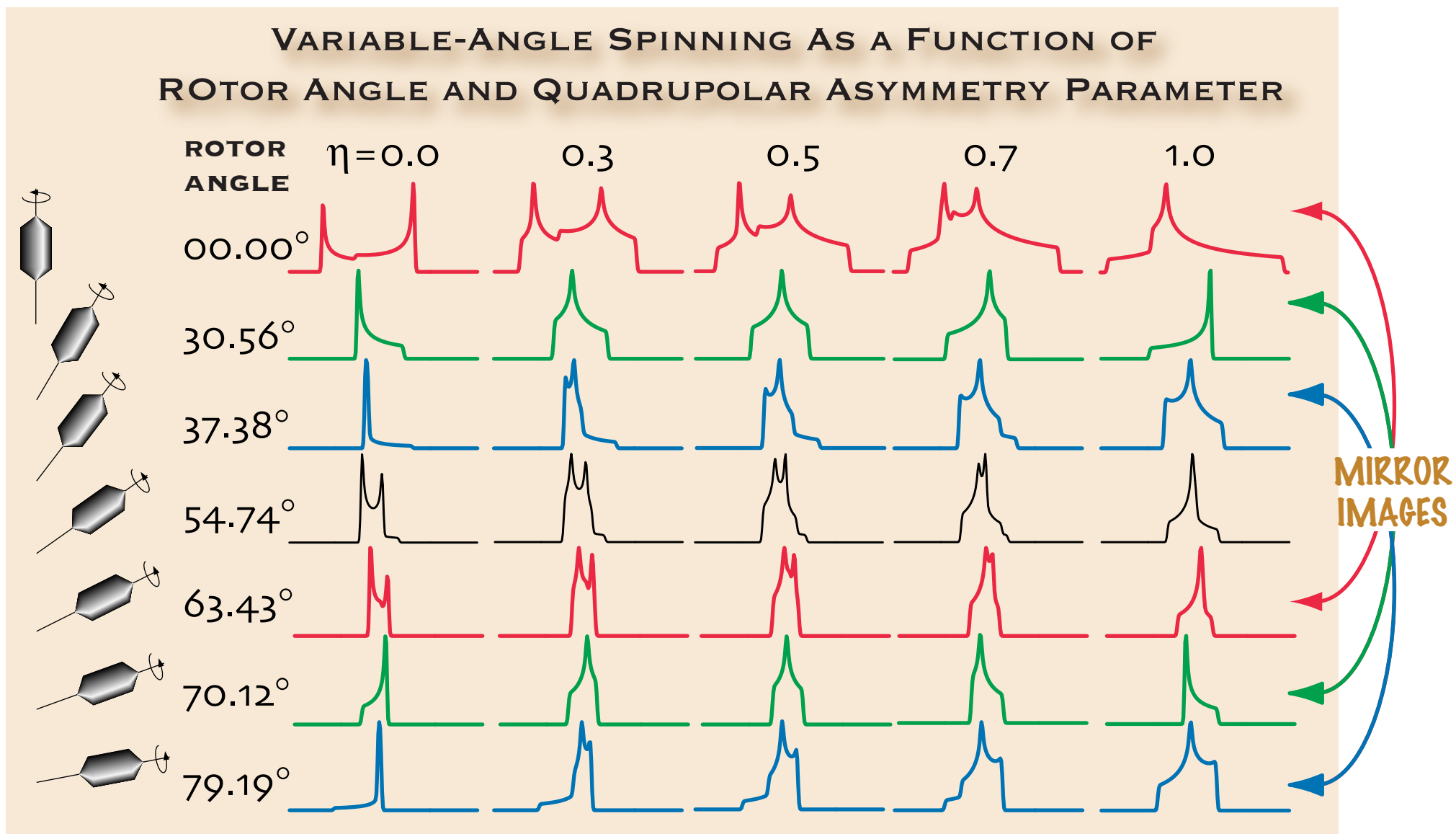
LET'S MAKE AN ECHO



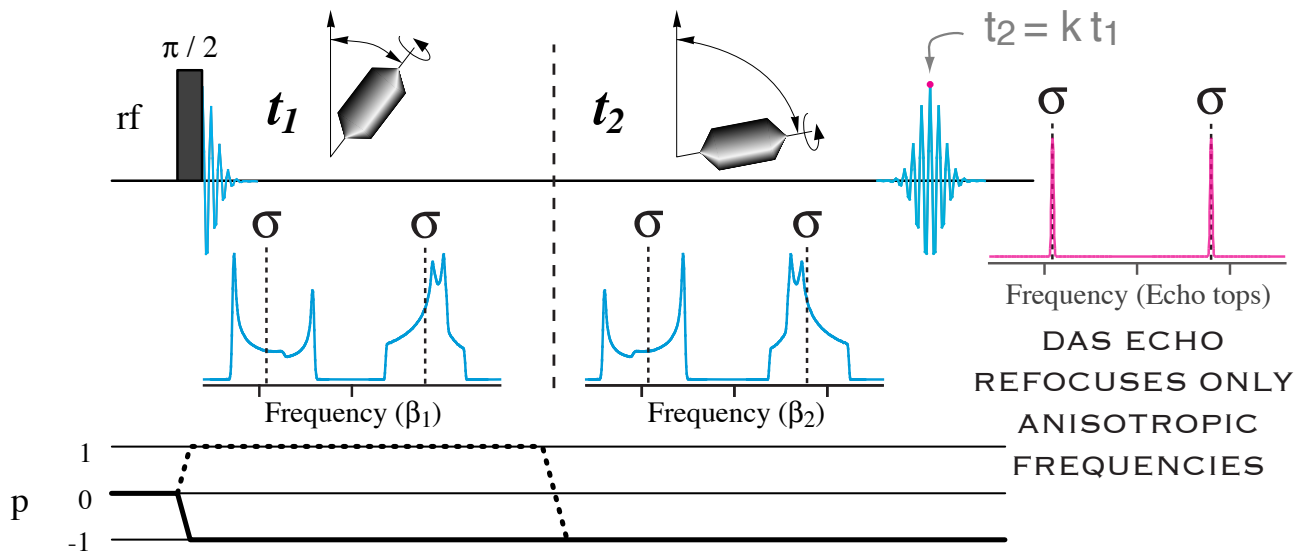
FIND MIRROR IMAGE

ANISOTROPIC LINESHAPES

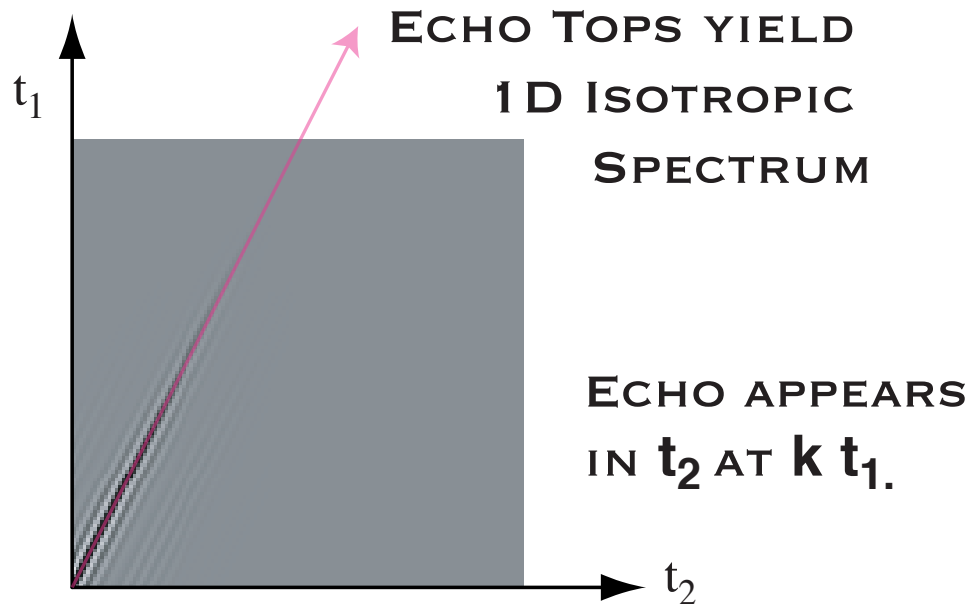
THE KEY TO UNDERSTANDING DYNAMIC-ANGLE SPINNING
(1988: FIRST HIGH RESOLUTION 2D METHOD FOR QUADRUPOLAR NUCLEI)



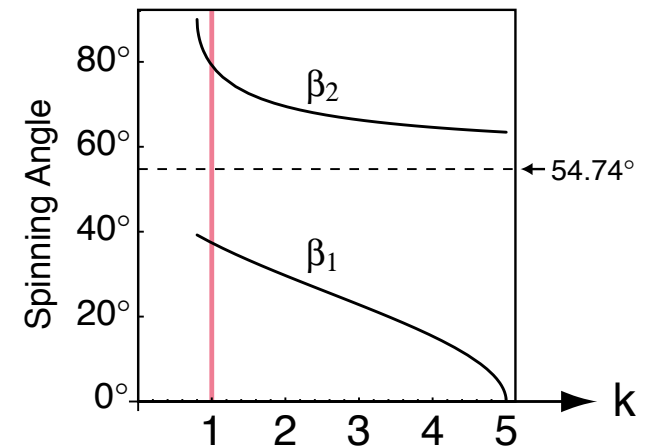
THE DAS ECHO



Chmelka et al.,
Nature, **339**, 42 (1989).
 Llor and Virlet,
Chem. Phys. Lett., **152**, 248 (1988).

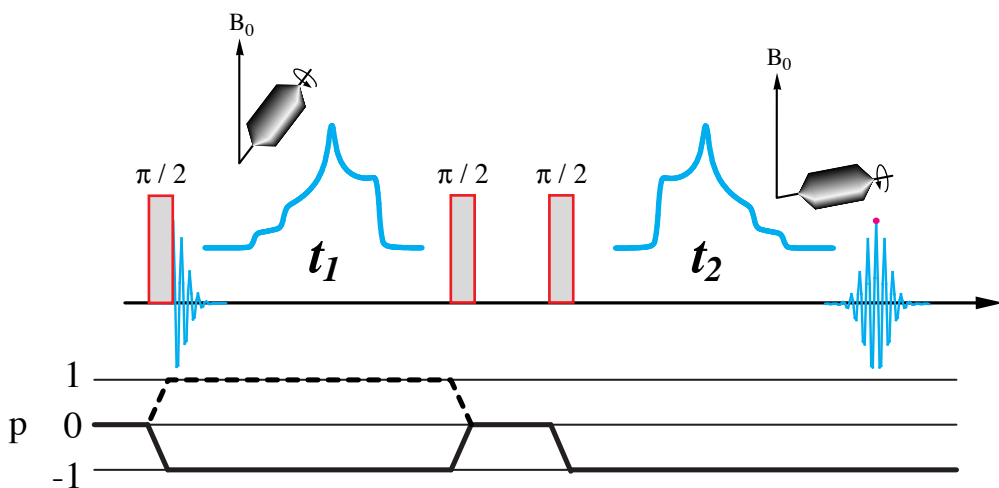


When does the echo occur in t_2 ?

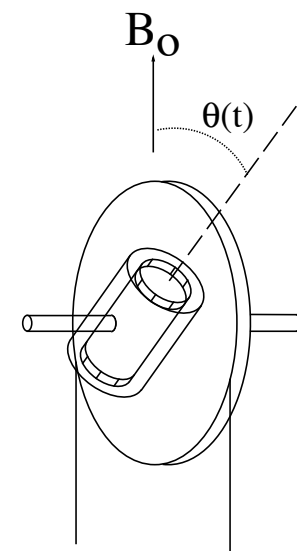


For example, with
 $\beta_1 = 37.38^\circ$, $\beta_2 = 79.19^\circ$
 we have $k = 1$

2D DYNAMIC ANGLE SPINNING

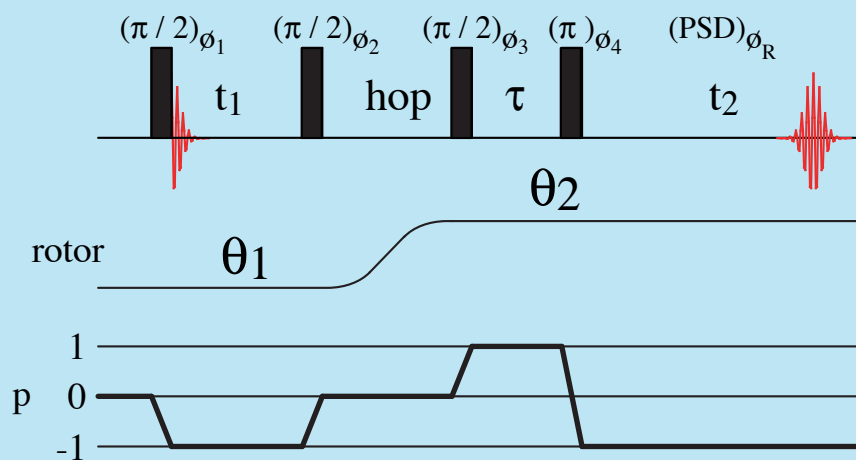


Mueller, Sun, Chingas, Zwanziger, Terao, and Pines, *J. Magn. Reson.*, **86**, 470 (1990).



SHIFTED ECHO ACQUISITION FOR PURE ABSORPTION MODE 2D SPECTRA IN SOLIDS

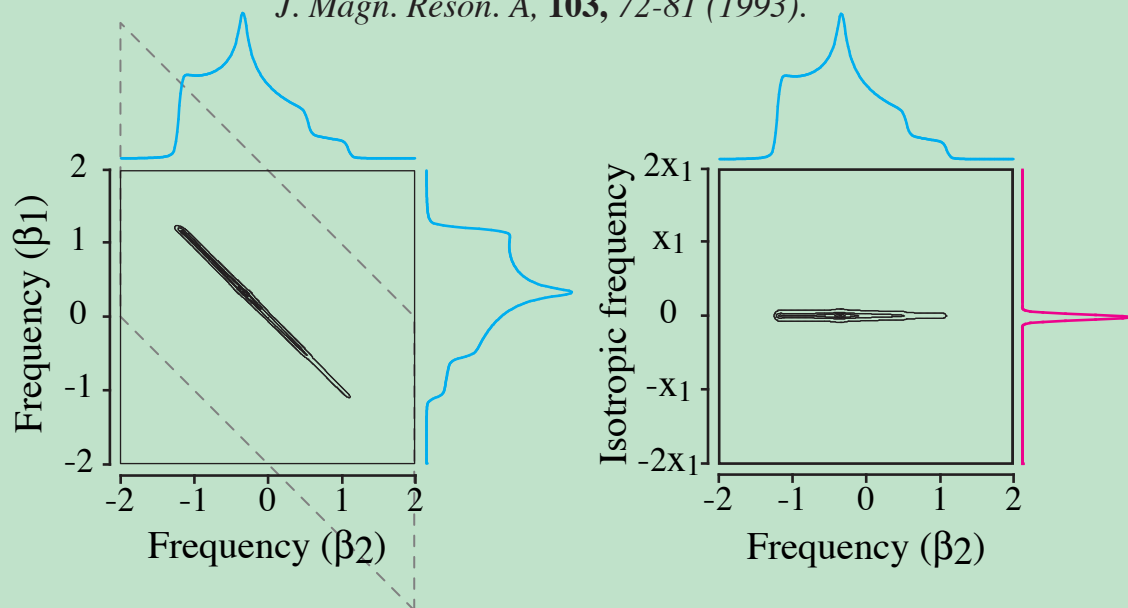
J. Magn. Reson. A, **103**, 72-81 (1993).



SHEARING TRANSFORMATION

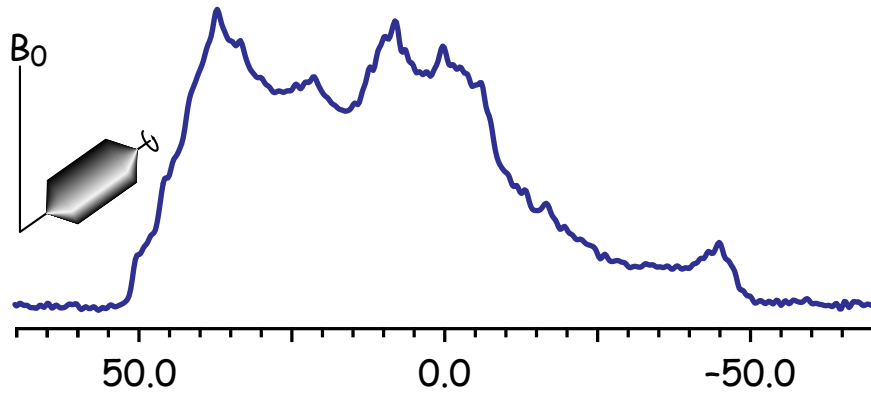
apply t_1 dependent 1st order phase correction to ω_2 dimension

J. Magn. Reson. A, **103**, 72-81 (1993).

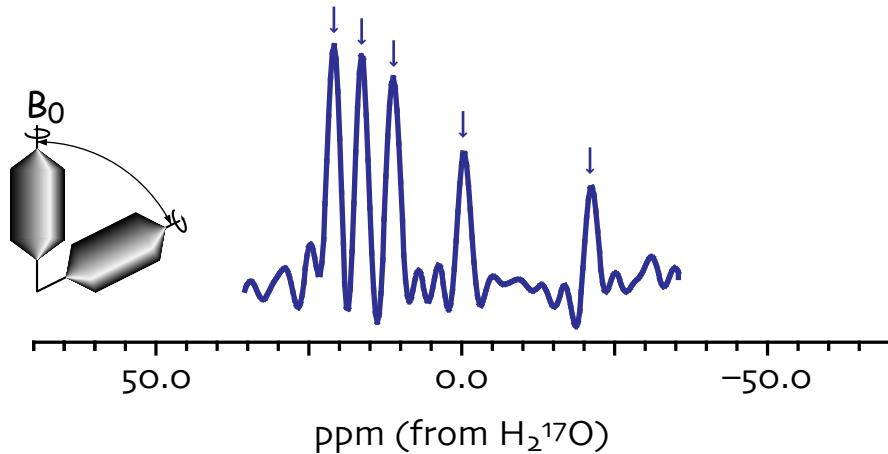


¹⁷O 2D DAS OF COESITE (A SiO₂ CRYSTALLINE POLYMORPH)

MAGIC-ANGLE SPINNING

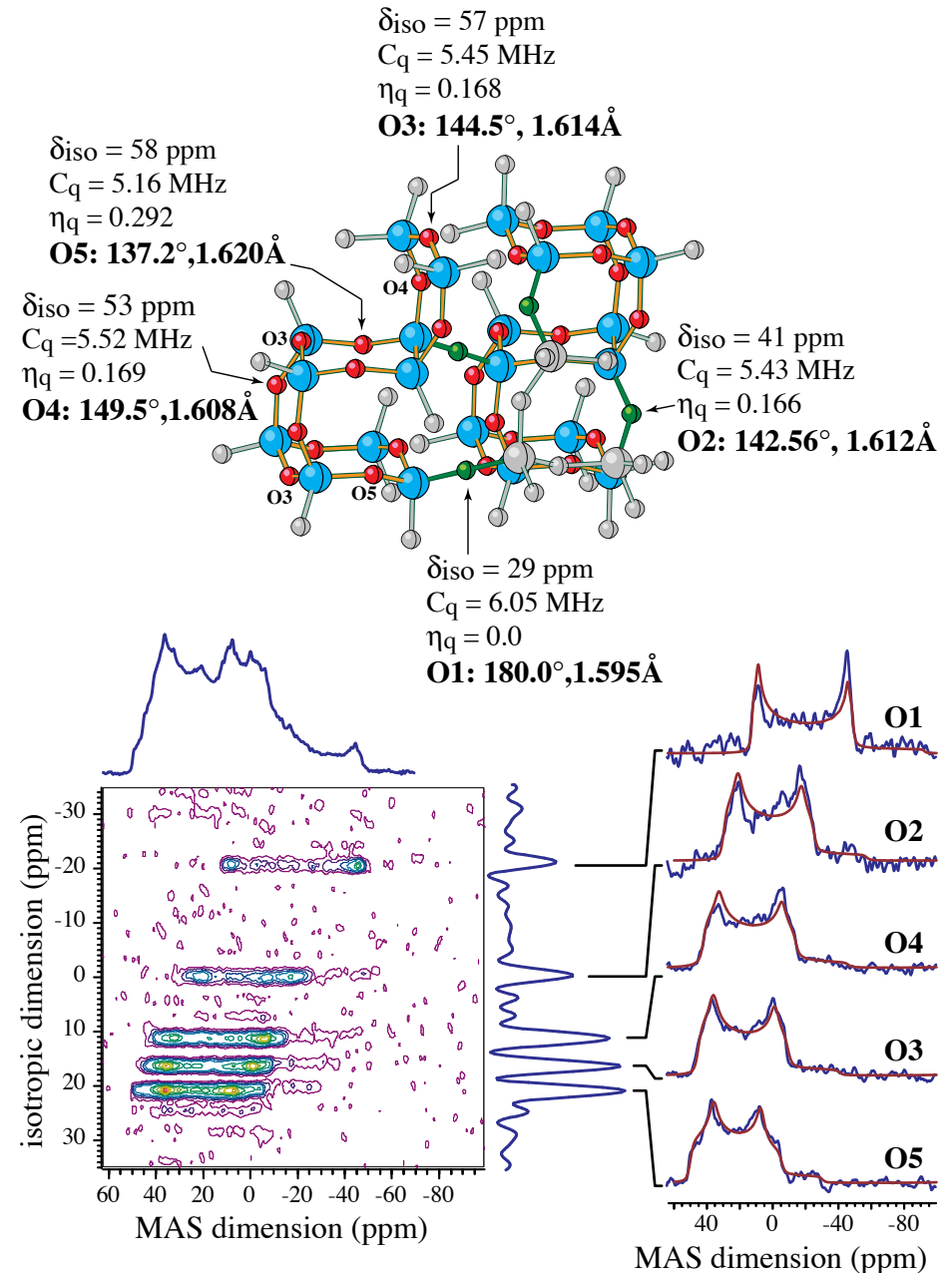


DYNAMIC-ANGLE SPINNING



J. Phys. Chem., **99**, 12341 (1995)

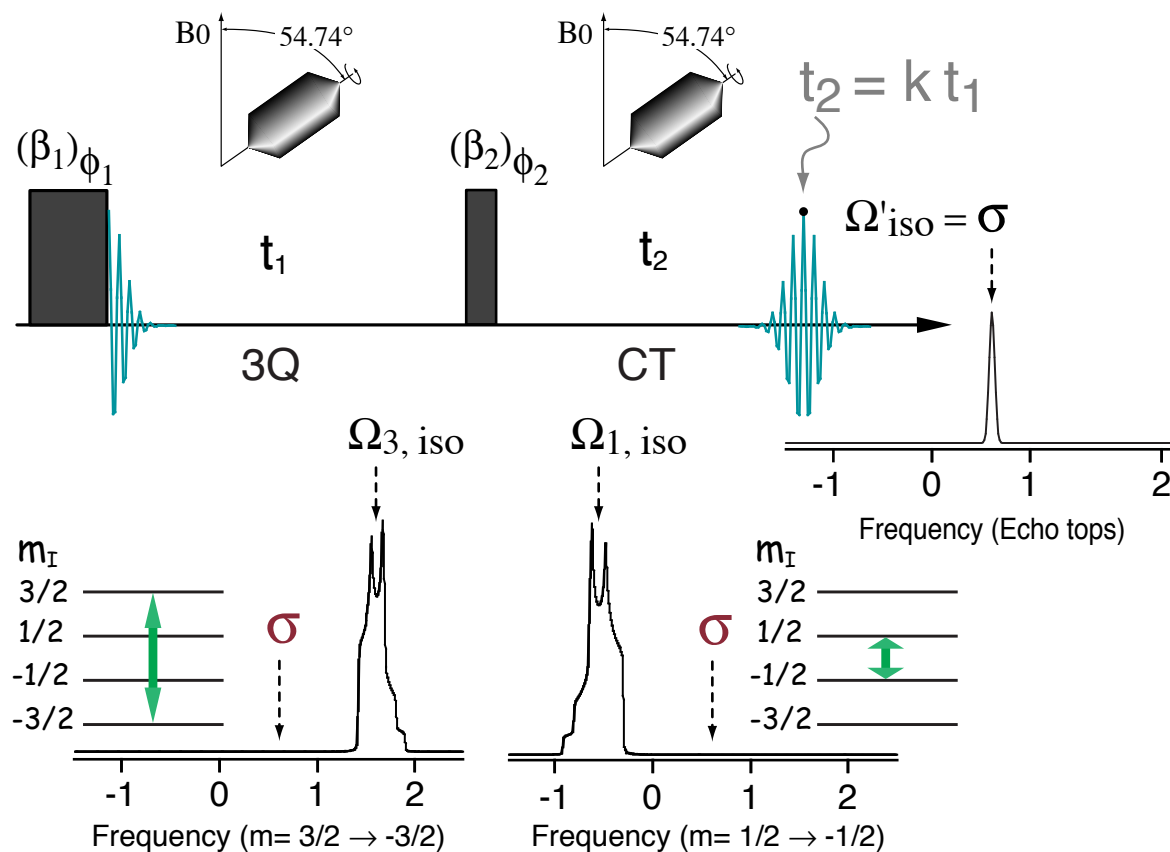
COESITE STRUCTURAL FRAGMENT



ANOTHER SOLUTION: THE MQ-MAS ECHO (HIGH RESOLUTION FOR THE PEOPLE)

**TRIPLE QUANTUM MAS SPECTRUM
IS THE MIRROR IMAGE OF THE
SINGLE QUANTUM MAS SPECTRUM**

Frydman and Harwood,
J. Am. Chem. Soc., **117**, 5367 (1995)
Medek, Harwood, and Frydman,
J. Am. Chem. Soc. **117**, 12779 (1995)

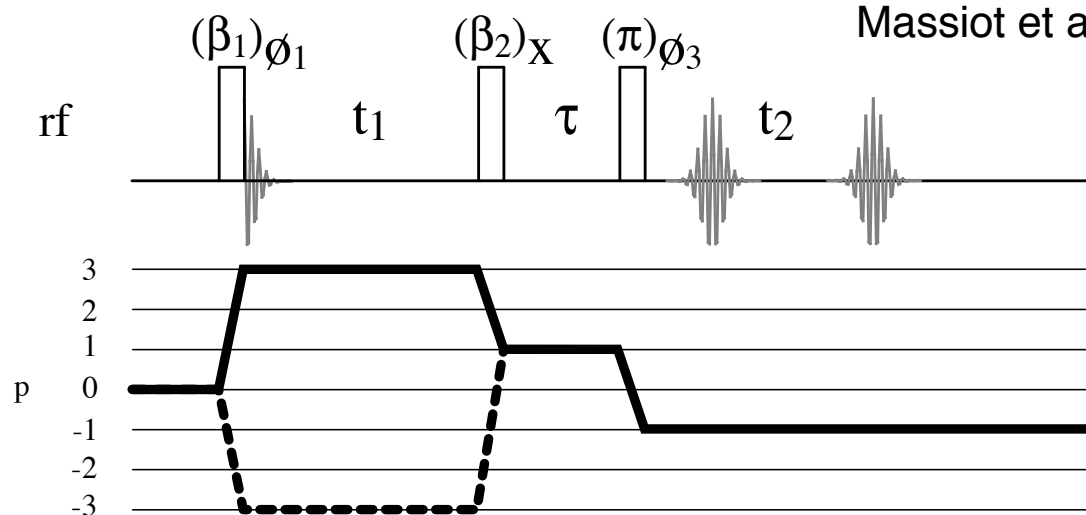


When does the echo occur in t_2 ?

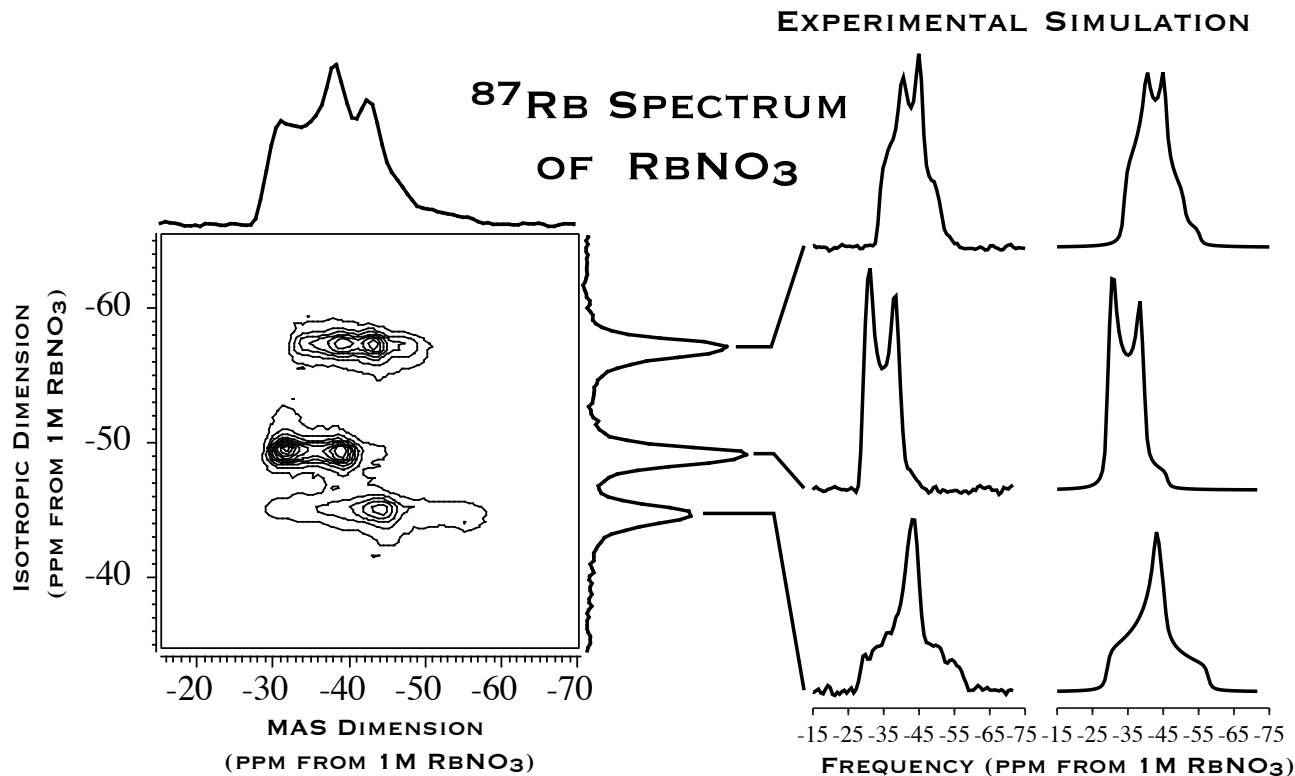
Spin	t1 transition ($m \rightarrow -m$)	k
3/2:	3QMAS	7/9
5/2:	3QMAS	19/12
	5QMAS	25/12
7/2:	3QMAS	101/45
	5QMAS	11/9
	7QMAS	161/45
9/2:	3QMAS	91/36
	5QMAS	95/36
	7QMAS	7/18
	9QMAS	31/6

2D SHIFTED-ECHO MQ-MAS

Massiot et al., *SSNMR*, **6**, 73 (1996)



AFTER
SHEARING
TRANSFORMATION:

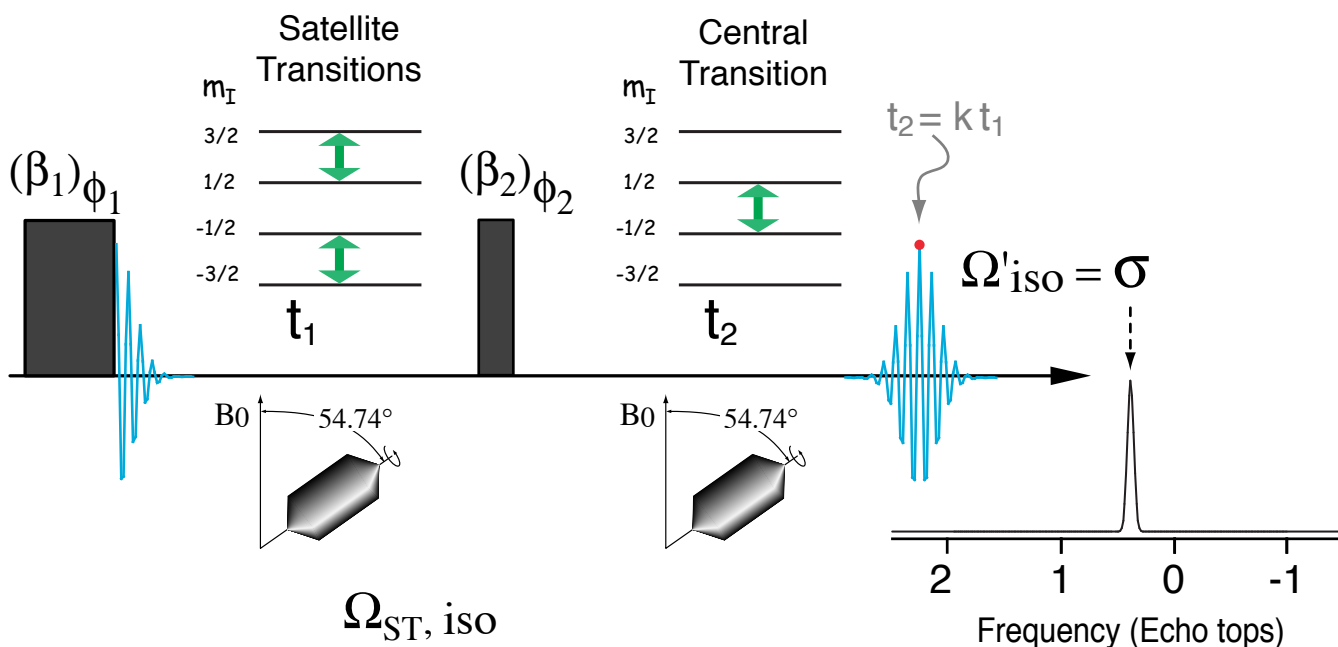


...AND ANOTHER SOLUTION: THE ST-MAS ECHO

Z. Gan, *J. Am. Chem. Soc.* 2000, **122**, 3242-3243

THE SATELLITE TRANSITION MAS SPECTRUM IS THE MIRROR IMAGE OF THE CENTRAL TRANSITION MAS SPECTRUM

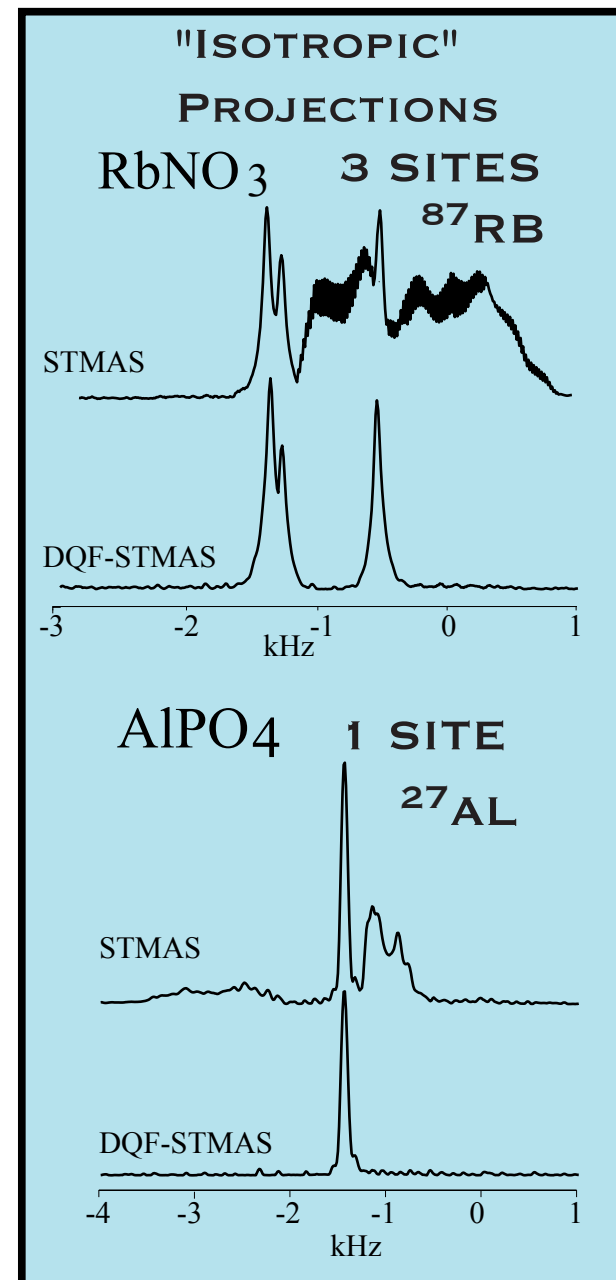
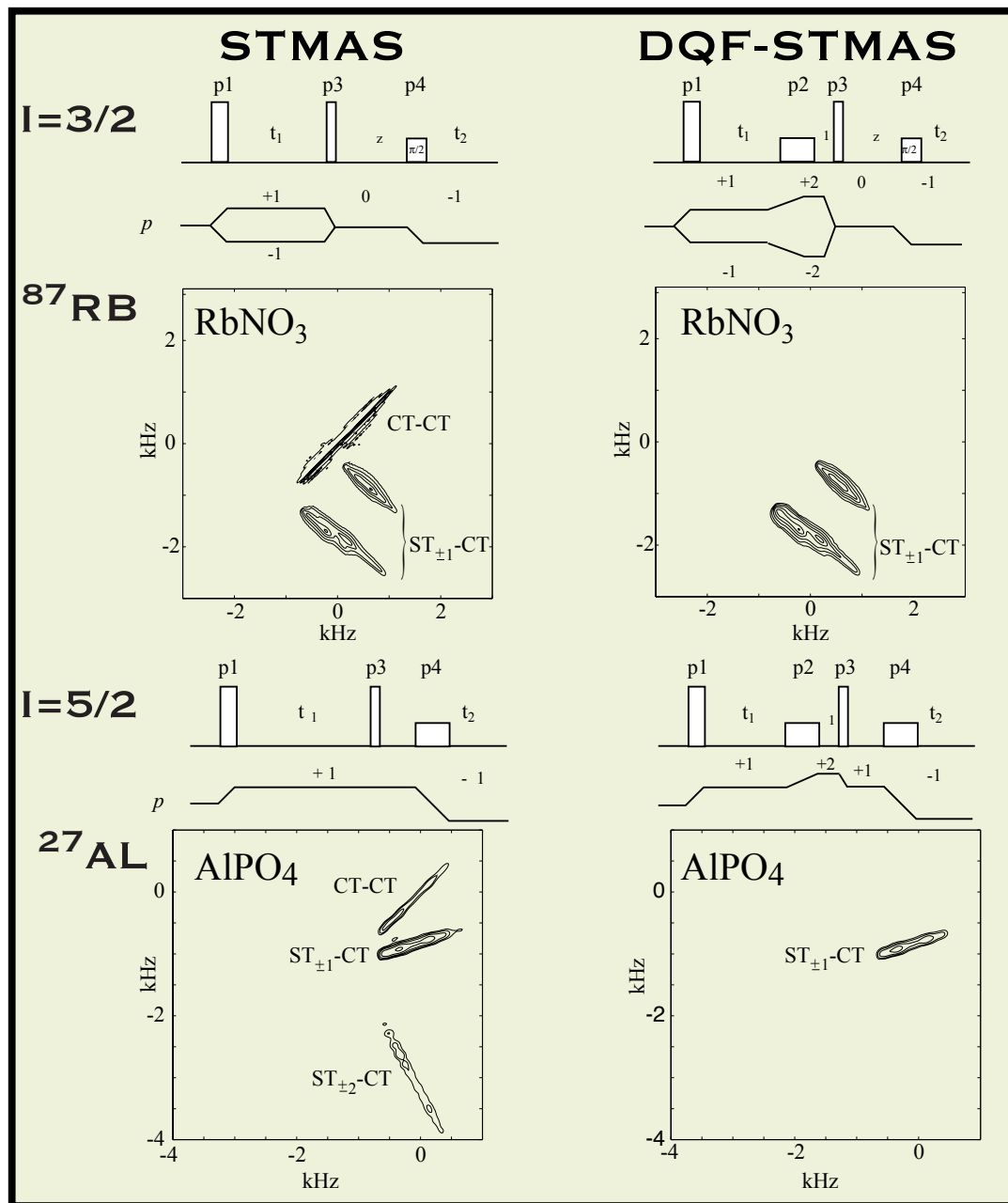
When does the echo occur in t_2 ?



Spin	t_1 transition	k
3/2:	1ST SATELLITES	8/9
5/2:	1ST SATELLITES	7/24
	2ND SATELLITES	11/6
7/2:	1ST SATELLITES	28/45
	2ND SATELLITES	23/45
	3RD SATELLITES	12/5
9/2:	1ST SATELLITES	55/72
	2ND SATELLITES	1/18
	3RD SATELLITES	9/8
	4TH SATELLITES	25/9

USE DOUBLE QUANTUM FILTERED ST-MAS TO ELIMINATE UNDESIRED CT-CT CORRELATION

Hyung-Tae Kwak and Zhehong Gan, *J. Magn. Reson.* **164** (2003) 369–372



ADVANTAGES**DISADVANTAGES****DOR:**

- **QUANTITATIVE**
- **HIGH SENSITIVITY**
- **LOW RF POWER**
- **ONE DIMENSIONAL EXPERIMENT**
 - **QUICK EXPERIMENT (IN PRINCIPLE)**

- **SPECIAL PROBE REQUIRED**
- **STABLE SPINNING REQUIRES FINESSE**
- **SLOW SPINNING SPEEDS**
 - **(LARGE # OF SIDEBANDS)**
- **LARGE COIL ... LOW RF POWER**
 - **POOR DECOUPLING.**

DAS:

- **QUANTITATIVE**
- **HIGH SENSITIVITY, EVEN WITH NUCLEI HAVING LARGE QUAD. COUPLINGS**
- **LOW RF POWER**
- **WORKS WELL FOR DILUTE QUADRUPOLEAR NUCLEI**

- **SPECIAL PROBE REQUIRED**
- **FAILS IN PRESENCE OF STRONG HOMONUCLEAR DIPOLAR COUPLINGS**
- **LONG HOP TIMES (30 MS) LIMITS USE TO SAMPLES WITH LONG LONGITUDINAL RELAXATION.**

MQ-MAS:

- **EASIEST TO IMPLEMENT (NO SPECIAL PROBE)**
- **WORKS WELL FOR ABUNDANT NUCLEI**
- **WORKS WELL FOR NUCLEI WITH SHORT LONGITUDINAL RELAXATION**

- **NOT ALWAYS QUANTITATIVE**
- **REQUIRES HIGH RF POWER FOR EXCITATION AND MIXING**
- **POOR SENSITIVITY FOR LARGE C_Q**
- **COMPLEX SPINNING SIDEBAND BEHAVIOR**

ST-MAS:

- **EASY TO IMPLEMENT (NO SPECIAL PROBE)**
- **EXCITES ONLY SINGLE QUANTUM TRANSITIONS**
- **WORKS WELL FOR ABUNDANT NUCLEI**
- **WORKS WELL FOR NUCLEI WITH SHORT LONGITUDINAL RELAXATION**

- **SENSITIVE TO MAGIC-ANGLE MISSET ($< 0.01^\circ$)**
- **STABLE SPINNING SPEED REQUIRED.**
- **REQUIRES HIGH RF POWER FOR SATELLITE EXCITATION.**
- **POOR SENSITIVITY FOR LARGE C_Q**
- **NOT ALWAYS QUANTITATIVE**
- **COMPLEX SPINNING SIDEBAND BEHAVIOR**
- **FAILS TO REMOVE 3RD AND OTHER HIGHER-ORDER EFFECTS**
- **FAILS WHEN THERE'S MOTIONAL AVERAGING OF SATELLITE LINESHAPES.**

A FEW LOOSE ENDS...

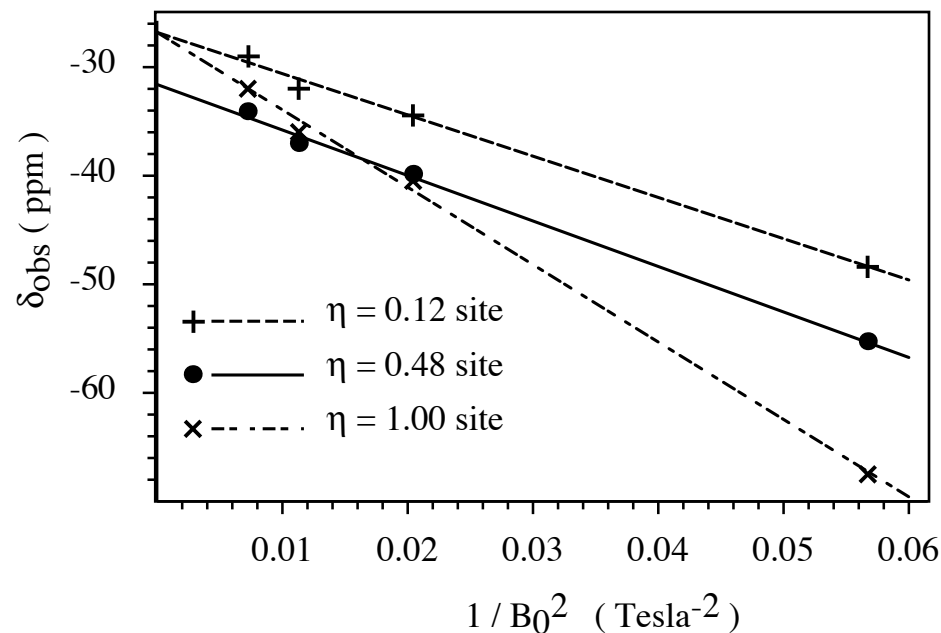
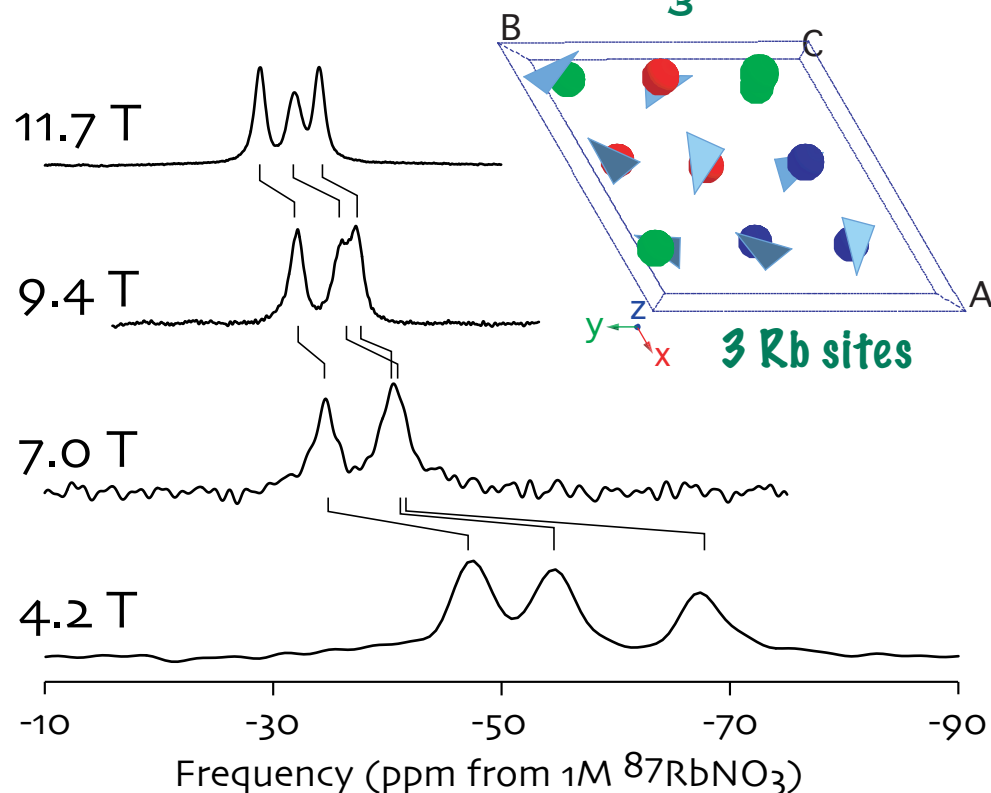
FIELD DEPENDANCE OF ISOTROPIC SHIFT

ISOTROPIC FREQUENCY OF QUADRUPOLAR NUCLEUS IS SUM OF ISOTROPIC
 (1) CHEMICAL SHIFT AND
 (2) 2ND ORDER QUADRUPOLAR SHIFT.

$$\Omega^{(iso)} = \delta_{iso}^{(CS)}(\text{ppm}) - \frac{1}{40} \frac{P_q^2}{\nu_0^2} \times 10^6 (\text{ppm})$$

$$P_q = C_Q(1 + \eta^2/3)^{1/2}$$

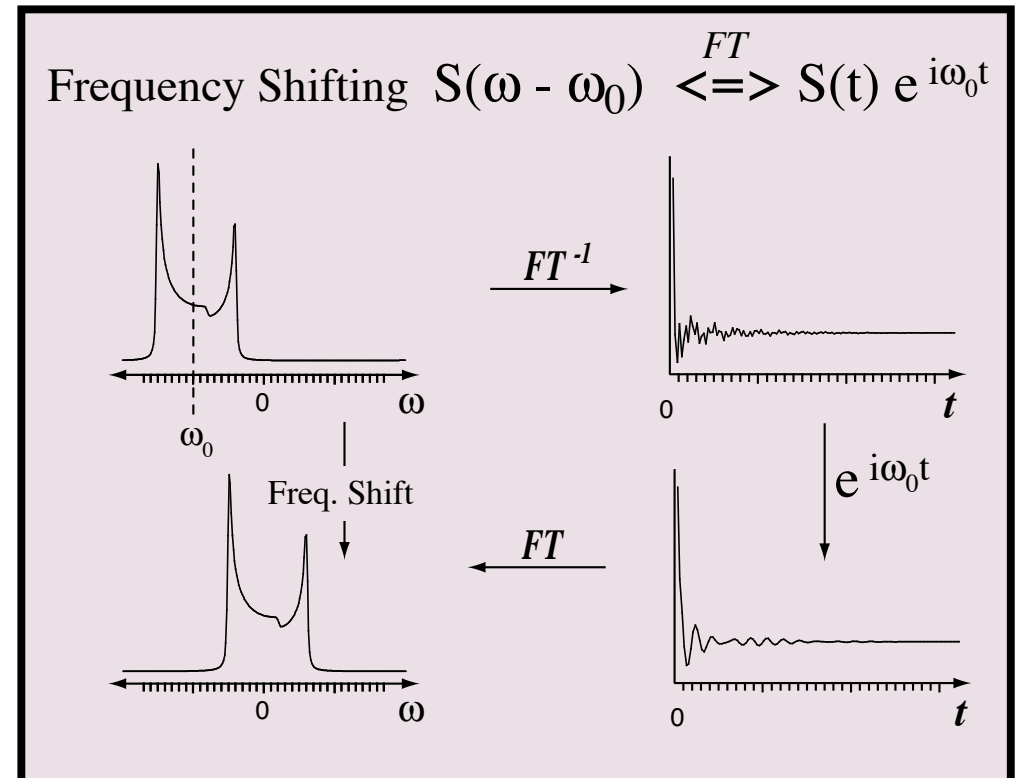
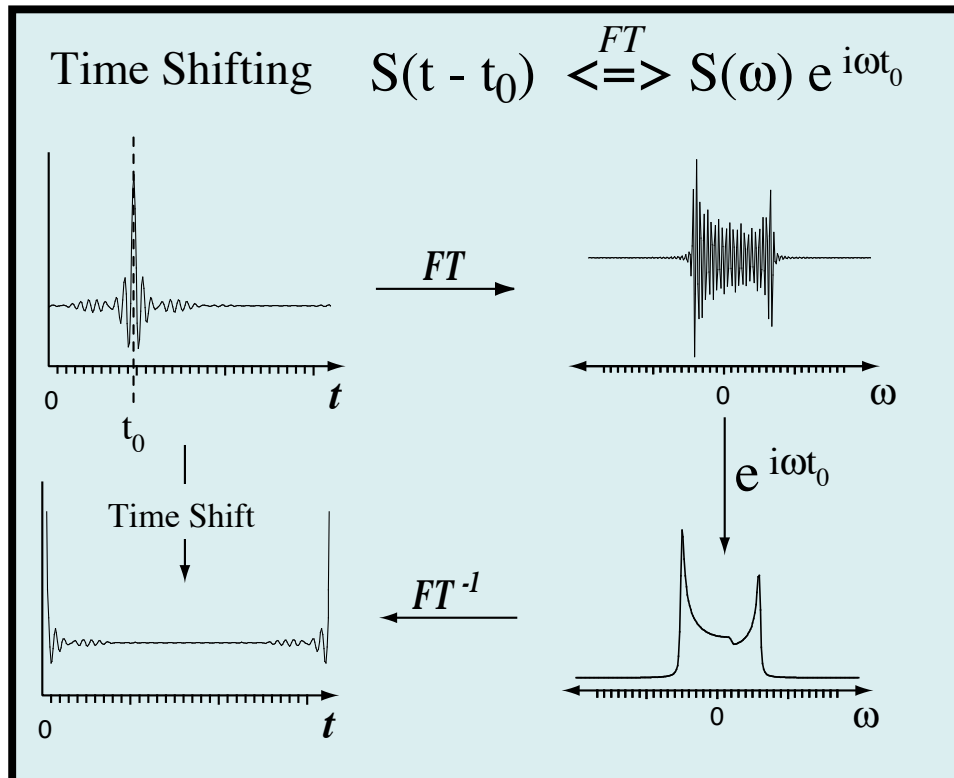
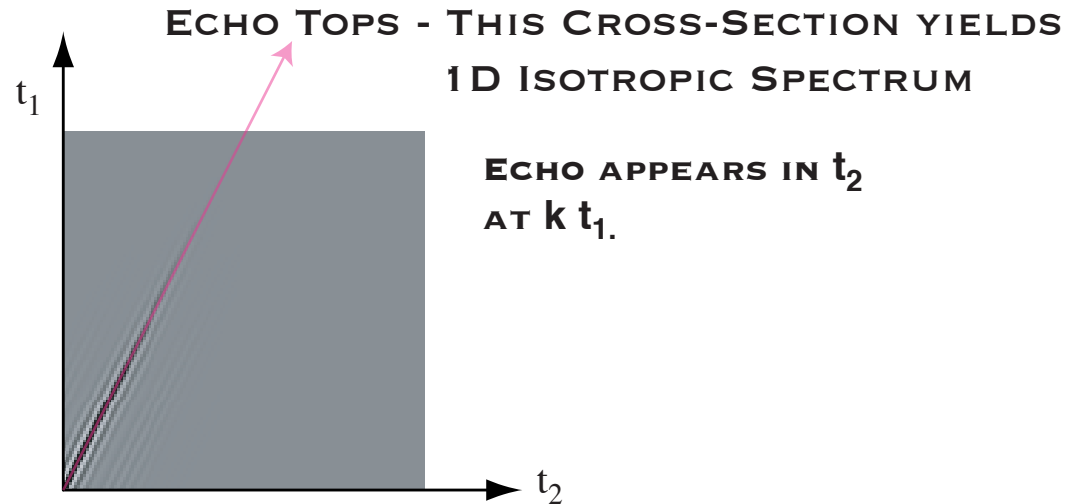
⁸⁷Rb DAS SPECTRA OF RbNO₃



Baltisberger, Gann, Wooten, Chang, Mueller, and Pines, *J. Am. Chem. Soc.*, 1992, **114**, 7489

WARNING: NEVER LABEL SPECTRUM AXIS OF QUADRUPOLAR NUCLEI IN SOLIDS AS "CHEMICAL SHIFT". ONLY TRUE IN LIMIT THAT P_q/V_0 GOES TO ZERO.

THE FOURIER TRANSFORM, SHIFT THEOREM, AND SHEARING TRANSFORMATIONS



SHEARING TRANSFORMATION IN DAS, MQ-MAS, ST-MAS

J. Magn. Reson. A, **103**, 72-81 (1993).

J. Magn. Reson. A, **102**, 195-204 (1993).

$$\mathbf{t}' = \mathbf{A}\mathbf{t}, \quad \text{where} \quad s'(\mathbf{t}) = s(\mathbf{A}\mathbf{t})$$

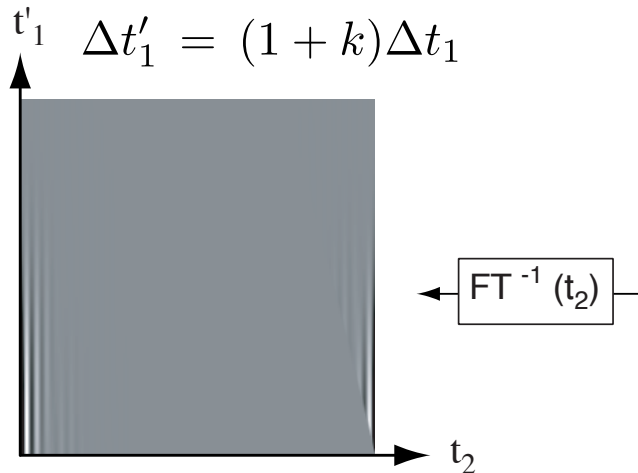
$$\mathbf{A} = \begin{pmatrix} 1+k & 0 \\ -k & 1 \end{pmatrix}$$

$$\tilde{\omega}' = \tilde{\omega}\mathbf{A}^{-1},$$

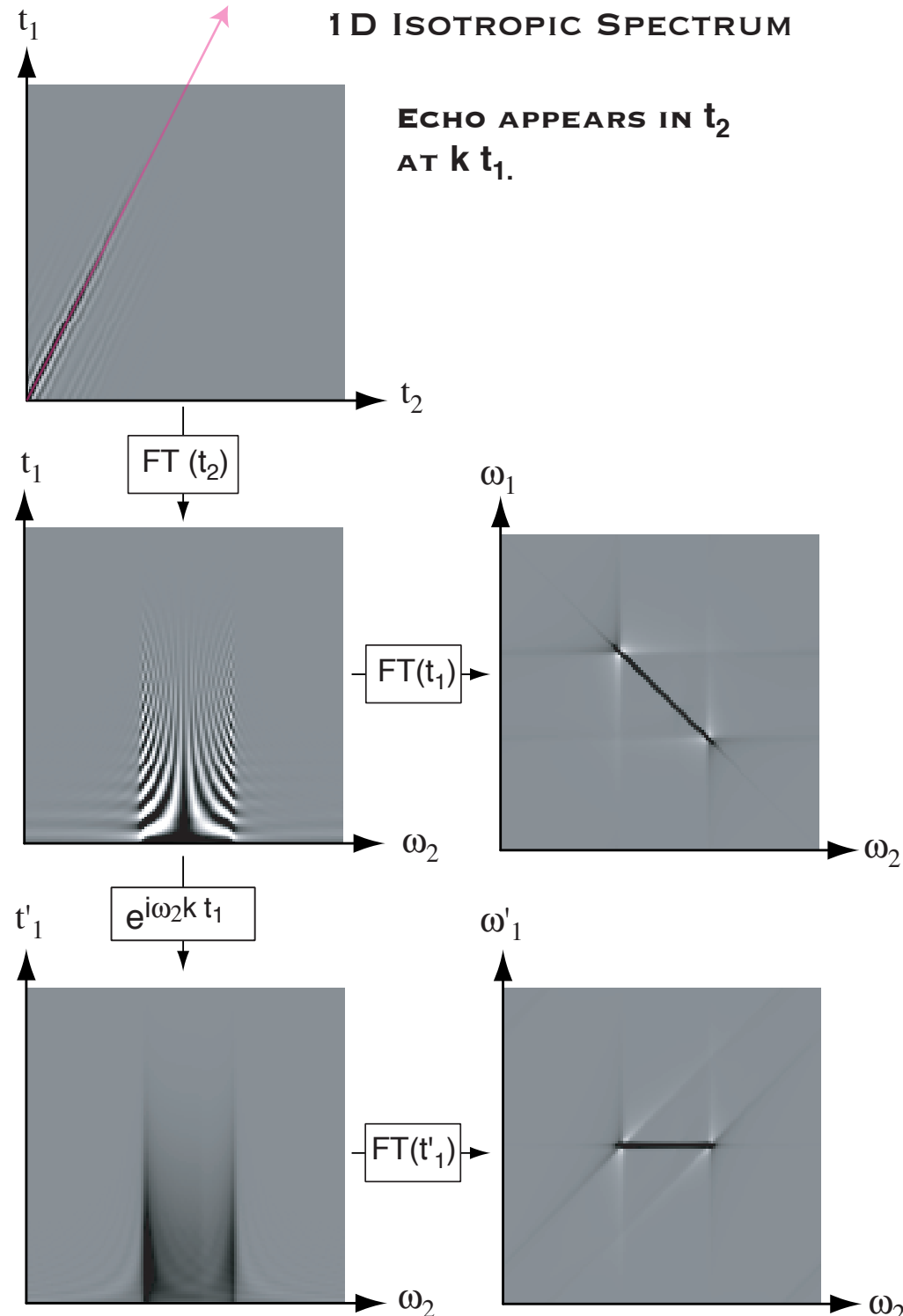
$$\text{where} \quad S'(\tilde{\omega}) = \frac{1}{|\mathbf{A}|} S(\tilde{\omega}\mathbf{A}^{-1})$$

$$t'_1 = (1+k)t_1$$

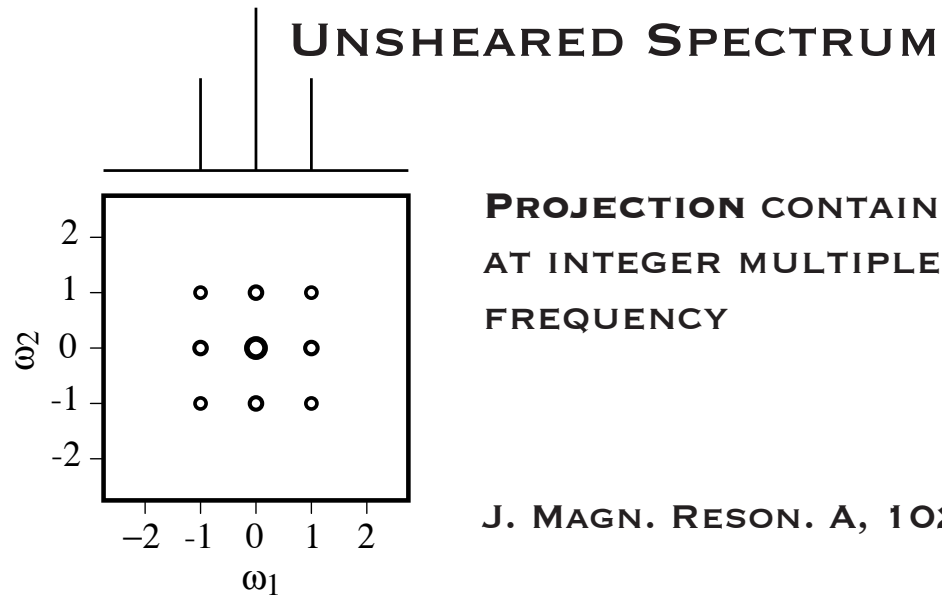
$$\Delta t'_1 = (1+k)\Delta t_1$$



ECHO TOPS - THIS CROSS-SECTION YIELDS
1D ISOTROPIC SPECTRUM



EFFECT OF SHEARING TRANSFORMATION ON SPINNING SIDEBANDS POSITIONS

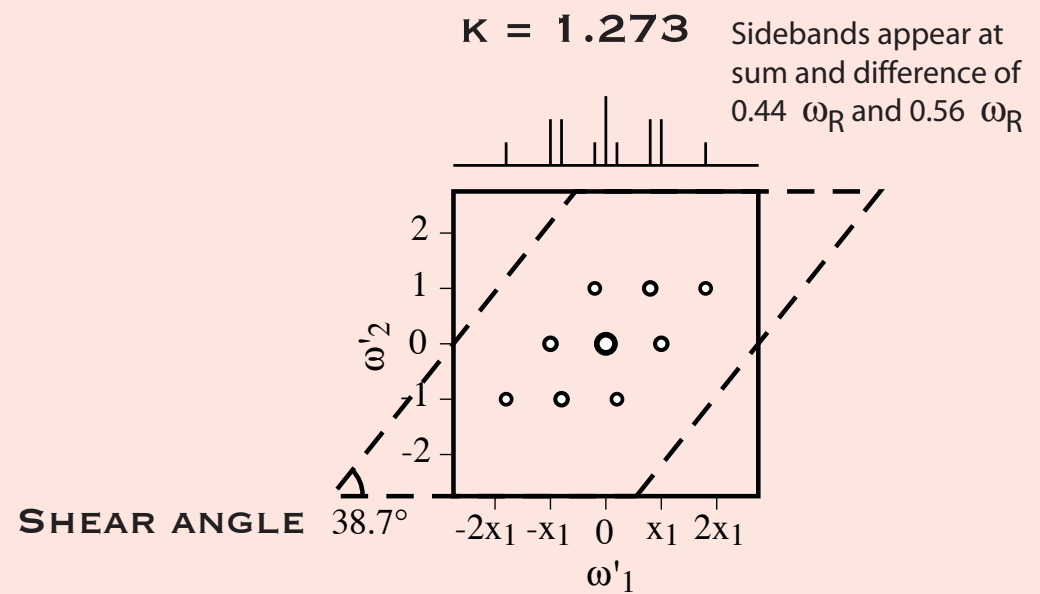
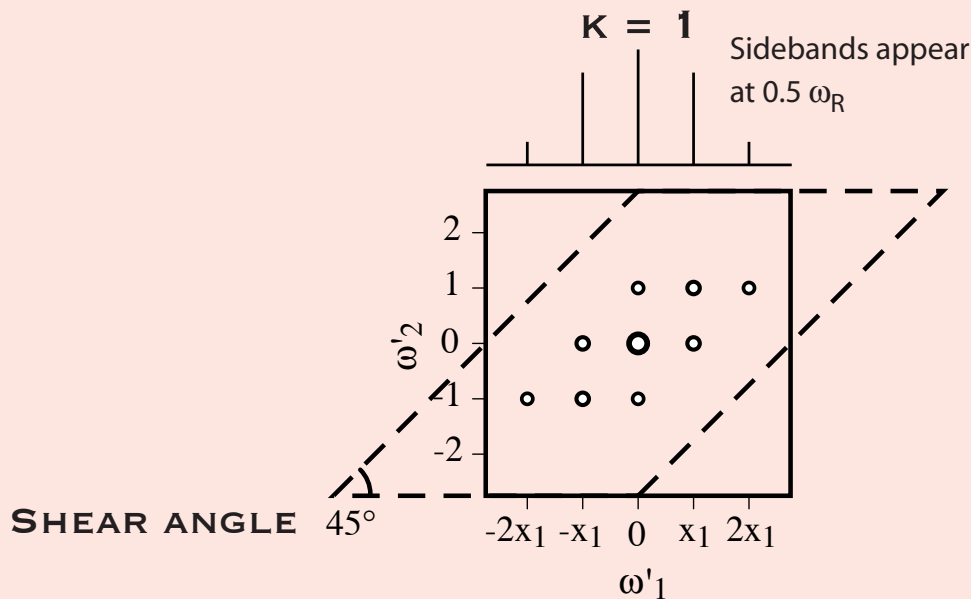


PROJECTION CONTAINS SIDEBANDS AT INTEGER MULTIPLES OF ROTOR FREQUENCY

J. MAGN. RESON. A, 102, 195-204 (1993)

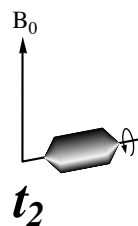
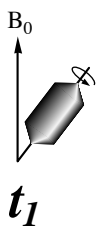
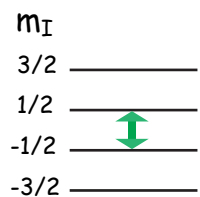
SHEARED SPECTRA

PROJECTION CONTAINS SIDEBANDS AT SUM/DIFFERENCE OF NON-INTEGER MULTIPLES OF ROTOR FREQUENCY

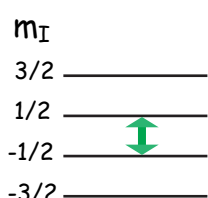
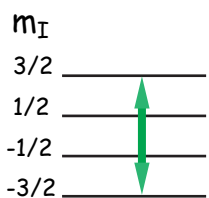
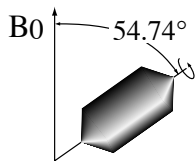


HYPERCOMPLEX PROCESSING OF DAS, MQ-MAS, ST-MAS

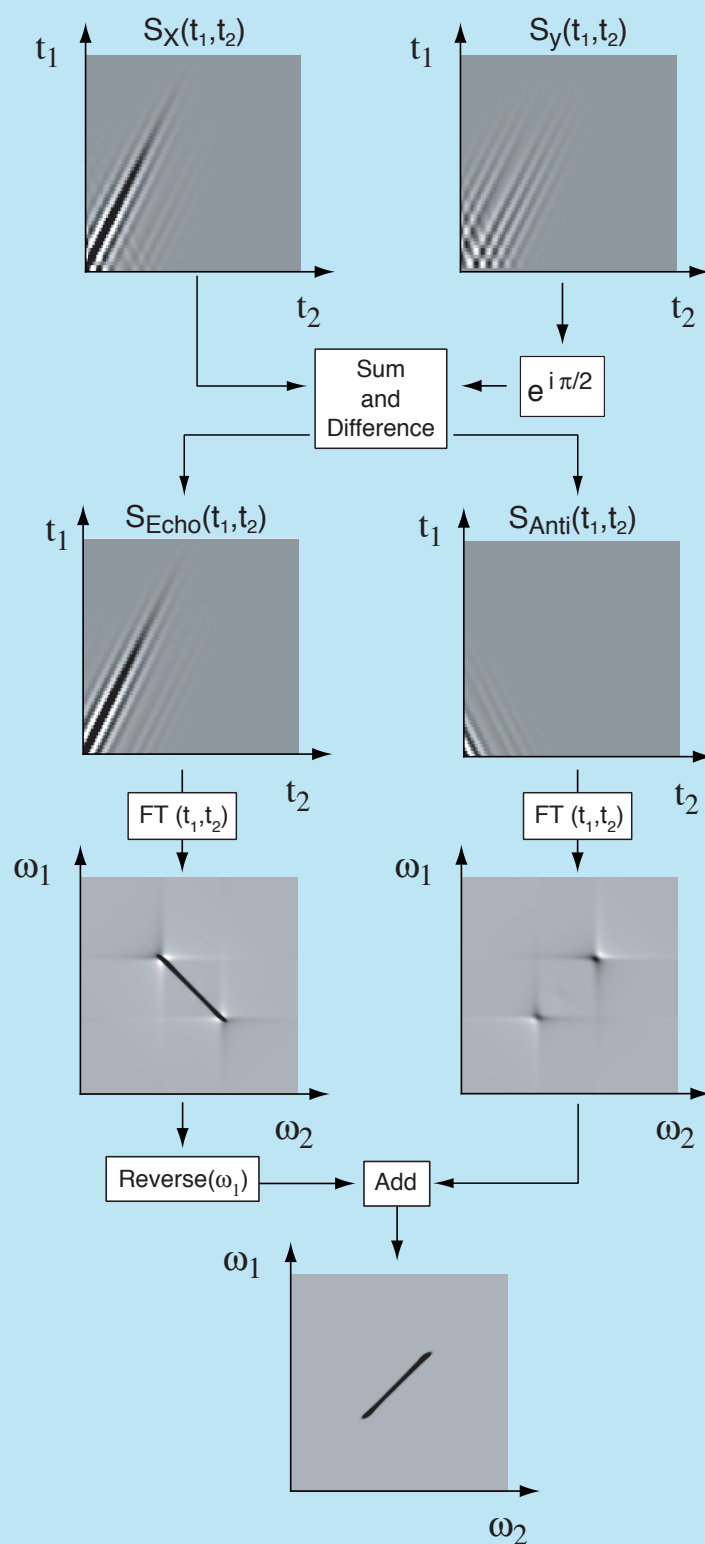
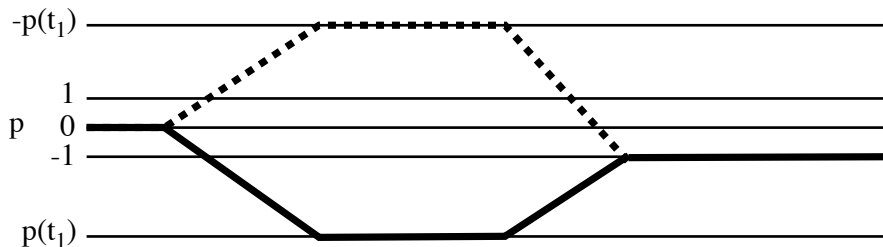
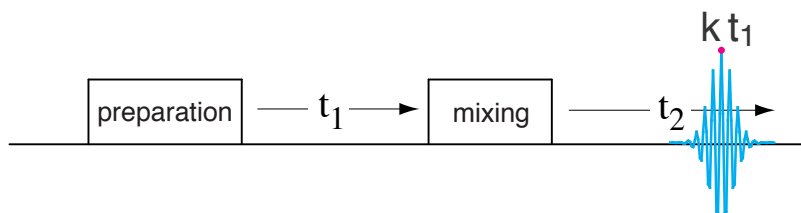
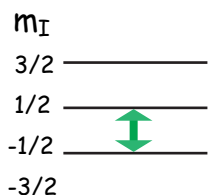
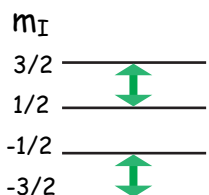
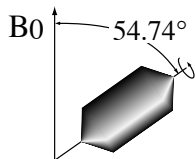
DAS



MQ-MAS



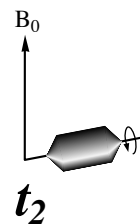
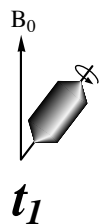
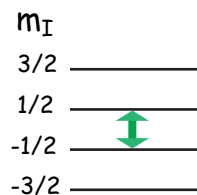
ST-MAS



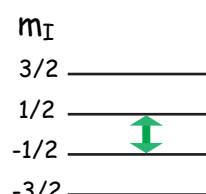
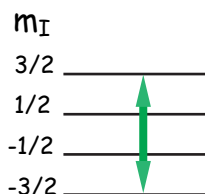
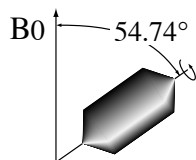
SHIFTED ECHO DATA ACQUISITION AND PROCESSING OF DAS, MQ-MAS, ST-MAS

J. Magn. Reson. A, **103**, 72-81 (1993).

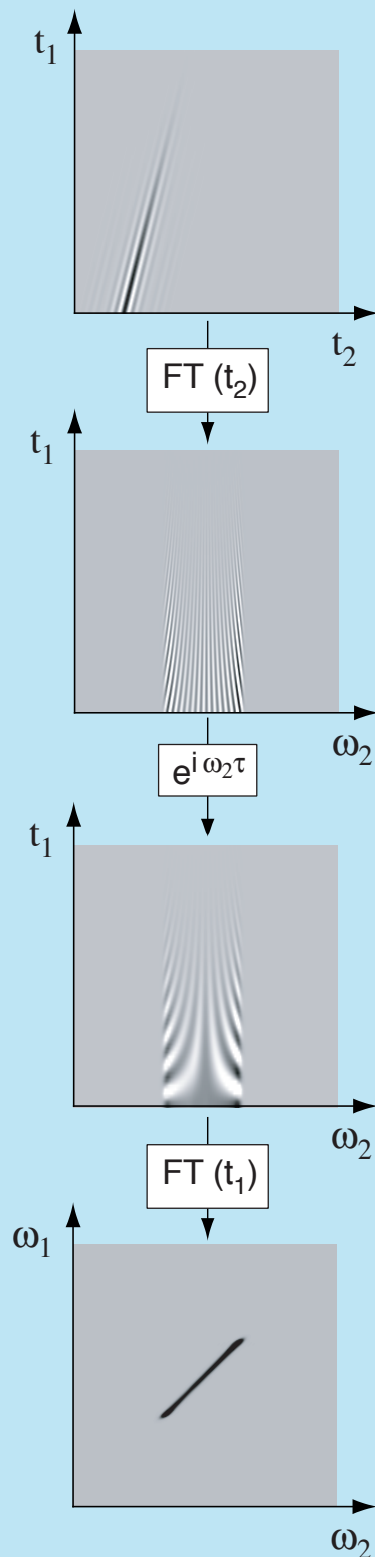
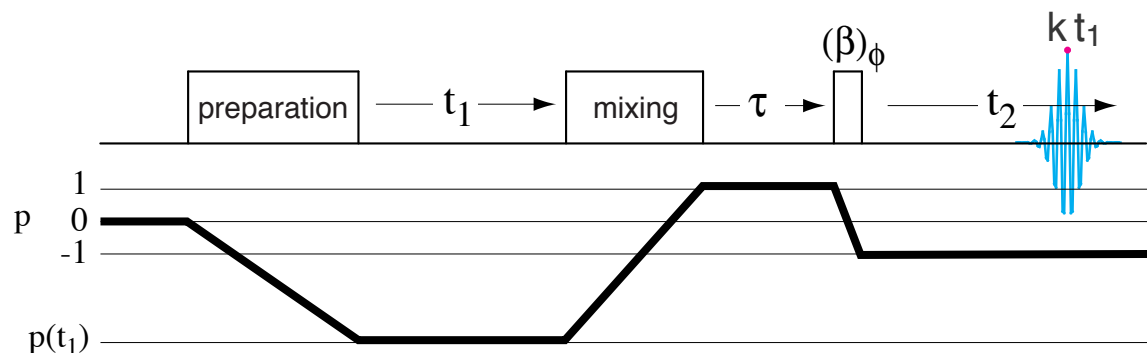
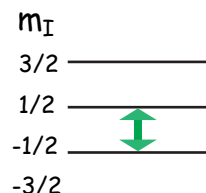
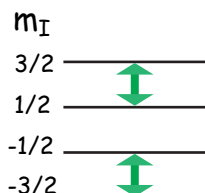
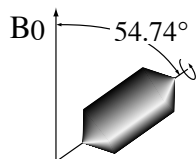
DAS



MQ-MAS



ST-MAS



PAY THE BILLS...

INTERPRETING QUADRUPOLAR COUPLINGS (ELECTRIC FIELD GRADIENTS)

$$H_q = \sum_k (-1)^k R_{2k}(\Omega_q) \left[\sqrt{\frac{3}{2}} \frac{eQ\gamma I}{I(2I-1)} T_{2-k} \right]$$

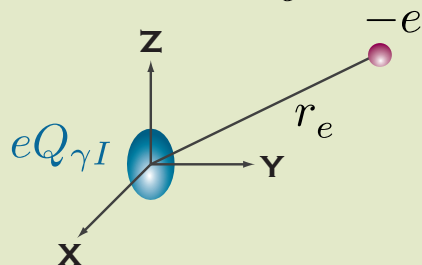
ELECTRIC FIELD GRADIENT AT THE NUCLEUS
NUCLEAR QUADRUPOLE MOMENT

ELECTRIC FIELD GRADIENT AT THE NUCLEUS

$$R_{2,k} = \sum_{\text{all electrons}} E_{2,k}(e) + \sum_{\text{all nuclei}} N_{2,k}(n)$$

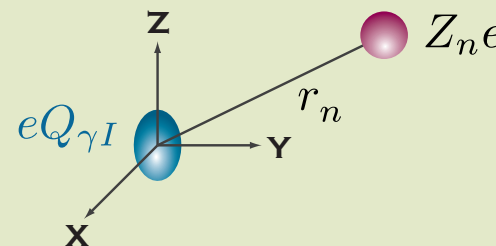
SURROUNDING ELECTRONS

$$E_{2,k}(e) = -e \sqrt{\frac{4\pi}{5}} \frac{1}{r_e^3} Y_{2,k}(\theta_e, \phi_e)$$



SURROUNDING NUCLEI

$$N_{2,k}(n) = Z_n e \sqrt{\frac{4\pi}{5}} \frac{1}{r_n^3} Y_{2,k}(\theta_n, \phi_n)$$



TOTAL ELECTRIC FIELD GRADIENT AT THE NUCLEUS

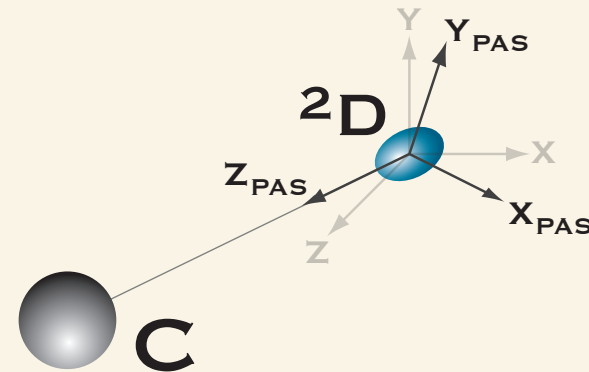
$$\langle R_{2,k} \rangle = \langle \Psi | R_{2,k} | \Psi \rangle$$

COMPLETE NUCLEAR AND ELECTRONIC WAVEFUNCTION

THE ELECTRIC FIELD GRADIENT TENSOR AND ITS ORIENTATION

- EFG IS 2ND RANK TRACELESS TENSOR: 5 ELEMENTS, $\langle R_{2,k} \rangle$, WITH $k = -2, -1, 0, 1, 2$.
- THERE EXISTS A PRINCIPAL AXIS COORDINATE SYSTEM (PAS) WHERE TENSOR IS DIAGONAL... $\langle R_{2,\pm 1}^{\text{PAS}} \rangle = 0$
- FURTHER DEFINE PAS SUCH THAT $|\langle R_{2,0}^{\text{PAS}} \rangle| > |\langle R_{2,\pm 2}^{\text{PAS}} \rangle|$
...LABELING PAS COMPONENTS AS $\langle \rho_{2,k} \rangle \equiv \langle R_{2,k}^{\text{PAS}} \rangle$

FOR EXAMPLE, IN A C-D BOND
THE 2D EFG PAS IS DIRECTED
ALONG THE C-D BOND AXIS.



- QUADRUPOLAR COUPLING CONSTANT AND ASYMMETRY PARAMETERS ARE DEFINED ...

$$C_q = 2 \frac{eQ}{h} \langle \rho_{2,0} \rangle \quad \text{and} \quad \eta_q C_q = 2\sqrt{6} \frac{eQ}{h} \langle \rho_{2,\pm 2} \rangle$$

IN CARTESIAN COORDINATES... $C_q = e^2 Q \langle q_{zz} \rangle / h$, and $\eta_q = \frac{\langle q_{xx} \rangle - \langle q_{yy} \rangle}{\langle q_{zz} \rangle}$

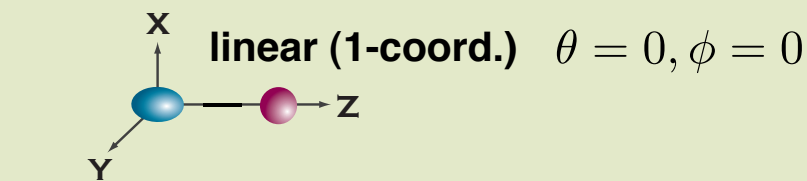
NOTE THAT... $\langle q_{zz} \rangle + \langle q_{yy} \rangle + \langle q_{xx} \rangle = 0$

POINT CHARGE MODEL FOR PREDICTING ELECTRIC FIELD GRADIENTS

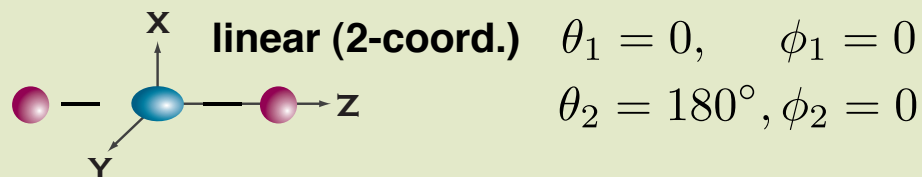
- NO ANALYTICAL EXPRESSION FOR EFG EXISTS WITHOUT APPROXIMATIONS.
- MOST DRASTIC IS THE POINT CHARGE MODEL: IT'S CRUDE, BUT OFTEN PROVIDES A QUALITATIVE UNDERSTANDING, AND WITH CALIBRATION CAN SOMETIMES BE QUANTITATIVE.

$$\langle R_{2,k} \rangle = \sum_{j=1}^n \frac{Z_j e}{d_i^3} \sqrt{\frac{4\pi}{5}} Y_{2,k}(\theta_j, \phi_j)$$

APPROXIMATE COORDINATING ATOMS AS POINT CHARGES AND CALCULATE SUM OF ALL COORDINATING ATOMS.



$$\langle R_{2,0} \rangle = \frac{Ze}{d^3}, \quad \langle R_{2,\pm 1} \rangle = 0, \quad \text{and} \quad \langle R_{2,\pm 2} \rangle = 0$$



$$\langle R_{2,0} \rangle = 2\frac{Ze}{d^3}, \quad \langle R_{2,\pm 1} \rangle = 0, \quad \text{and} \quad \langle R_{2,\pm 2} \rangle = 0$$

POINT CHARGE MODEL PREDICTS CQ DOUBLES, AND PAS UNCHANGED WHEN ATOM GOES FROM ONE TO TWO-COORDINATED LINEAR.

EXPERIMENTAL ^{17}O NMR MEASUREMENTS IN SILICATES

NON-BRIDGING OXYGEN $\text{Si-}^{17}\text{O}^-$

$\alpha\text{-Na}_2\text{Si}_2\text{O}_5$ $C_Q = 2.40$ MHz, $\eta = 0.20$

$\text{Li}_2\text{Si}_2\text{O}_5$ $C_Q = 2.45$ MHz, $\eta = 0.10$

BRIDGING OXYGEN $\text{Si-}^{17}\text{O-Si}$

$\alpha\text{-Na}_2\text{Si}_2\text{O}_5$ $C_Q = 5.74$ MHz, $\eta = 0.20$

$\text{Li}_2\text{Si}_2\text{O}_5$ $C_Q = 5.60$ MHz, $\eta = 0.10$

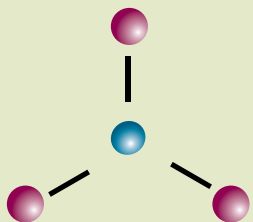
Maekawa, Florian, Massiot, Kiyono, Nakamura, *J. Phys. Chem.* 1996, **100** (17), 5525-5532.

Xue, Stebbins, Kanzaki, *Am. Miner.* 1994, **79**, 31.

POINT CHARGE MODEL FOR PREDICTING ELECTRIC FIELD GRADIENTS

Trigonal Planar

Place quadrupole nucleus at the origin and the z-axis perpendicular to the plane containing 3 point charges

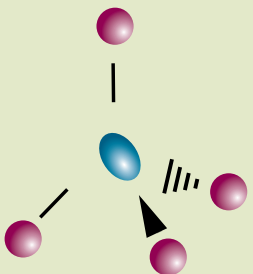


$$\theta = 90^\circ, \phi = 0, \pm 120^\circ$$

$$\langle R_{2,0} \rangle = -\frac{3Ze}{2d^3}, \quad \langle R_{2,\pm 1} \rangle = 0, \quad \text{and} \quad \langle R_{2,\pm 2} \rangle = 0$$

- z-axis of efg PAS is perpendicular to plane containing nucleus and coordinating charges.
- Asymmetry parameter is zero, and sign of the quadrupole coupling constant is opposite to linear cases.

Tetrahedral



$$\langle R_{2,0} \rangle = 0, \quad \langle R_{2,\pm 1} \rangle = 0, \quad \text{and} \quad \langle R_{2,\pm 2} \rangle = 0$$

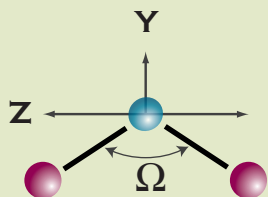
¹¹B Examples from Borosilicates...

	<u>C_Q</u>	<u>ETA</u>	
TRIGONAL PLANAR ¹¹ BO ₃ (RING)	2.65 MHz	0.20	LIN-SHU DU AND JONATHAN F. STEBBINS, <i>J. Non-Cryst. Solids</i> 315 (2003) 239–255
TRIGONAL PLANAR ¹¹ BO ₃ (NON-RING)	2.55 MHz	0.20	
TETRAHEDRAL ¹¹ BO ₄ (1B,3SI)	0.30 MHz	0.00	
TETRAHEDRAL ¹¹ BO ₄ (0B 4SI)	0.30 MHz	0.00	

POINT CHARGE MODEL FOR PREDICTING ELECTRIC FIELD GRADIENTS

Bent

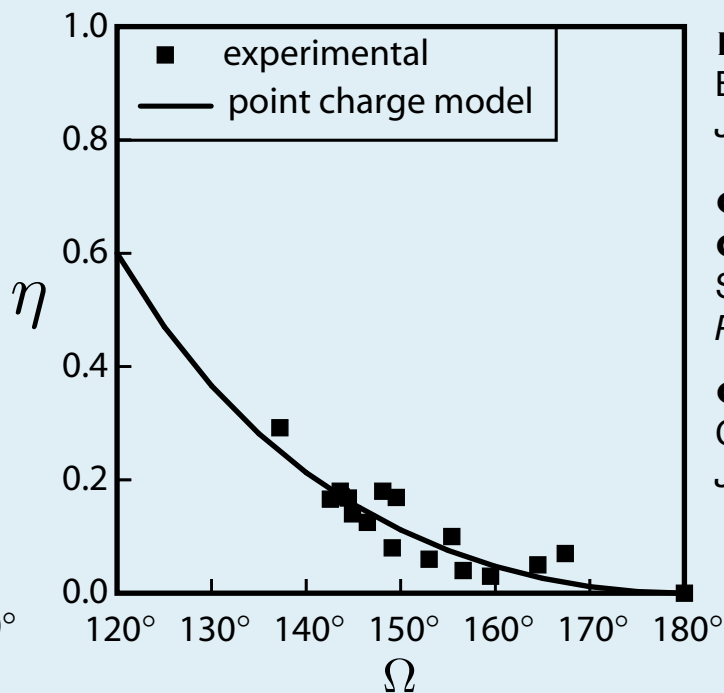
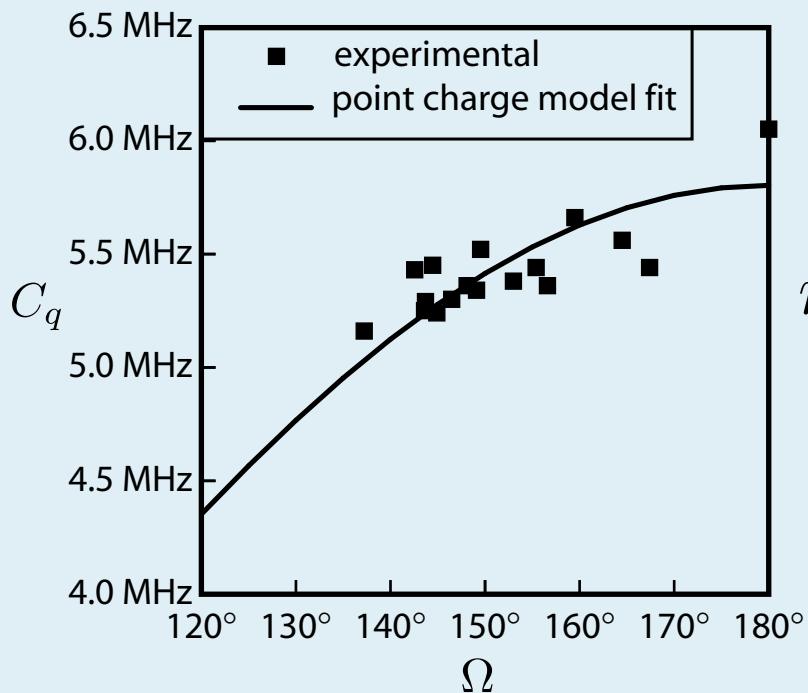
Place quadrupole nucleus at the origin with z-axis in plane containing atoms and perpendicular to the angle bisector



$$\langle R_{2,0} \rangle = \frac{Ze}{d^3} (3 \sin^2 \Omega/2 - 1), \quad \langle R_{2,\pm 1} \rangle = 0, \quad \text{and} \quad \langle R_{2,\pm 2} \rangle = \frac{Ze}{d^3} \sqrt{\frac{3}{2}} \cos^2 \Omega/2$$

$$C_q = 2 \frac{e^2 Q}{h} \frac{Z}{d^3} (1 - \cos \Omega) \quad \text{and} \quad \eta = -\frac{3(\cos \Omega + 1)}{3 \cos \Omega - 1}$$

¹⁷O QUADRUPOLAR COUPLING PARAMETERS IN SI-¹⁷O-SI LINKAGE AS A FUNCTION OF SI-O-SI ANGLE



FERRIERITE - 10 SITES

Bull et al,
J. Am. Chem. Soc. **122** (2000) 4948



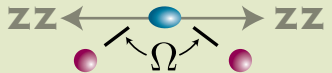
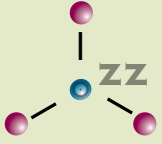
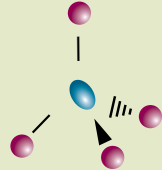
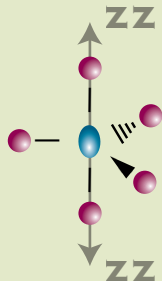
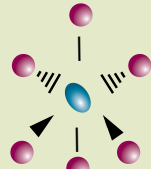
CRISTOBALITE - 1 SITE

Spearing et al,
Phys. Chem. Min. **19** (1992) 307

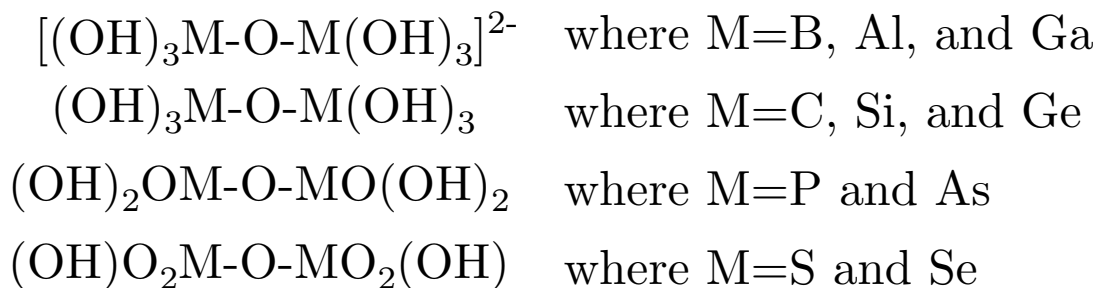
COESITE - 5 SITES

Grandinetti, et al,
J. Phys. Chem. **99** (1995) 12341

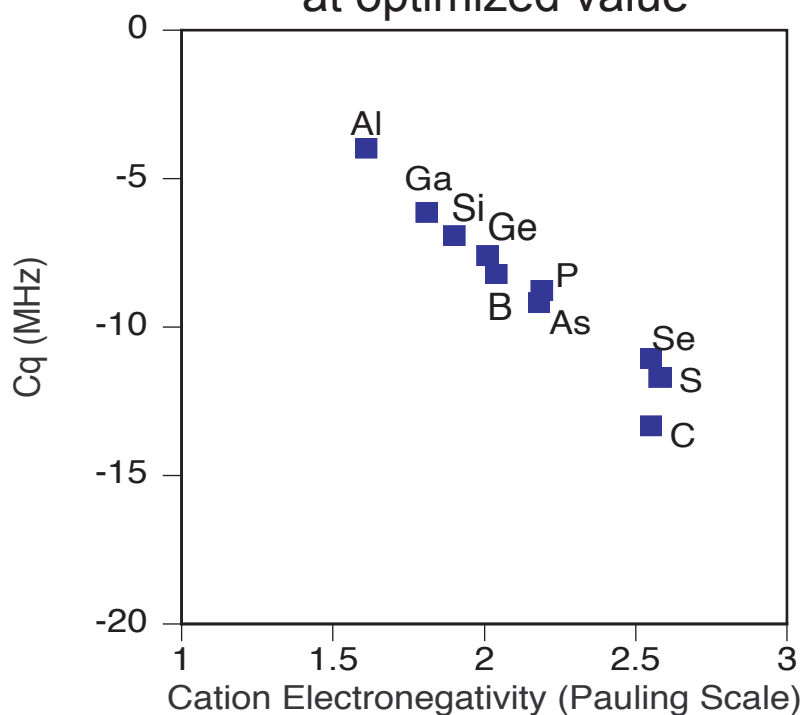
ROUGH GUIDE TO SOME POINT CHARGE MODELS FOR EFG

Name	Structure	C_q	η_q
linear (1)		$2 \frac{e^2 Q}{h} \frac{Z}{d^3}$	0
linear (2)		$4 \frac{e^2 Q}{h} \frac{Z}{d^3}$	0
bent (2)		$2 \frac{e^2 Q}{h} \frac{Z}{d^3} (1 - \cos \Omega)$	$-\frac{3(\cos \Omega + 1)}{3 \cos \Omega - 1}$
Trigonal Planar (3)		$-3 \frac{e^2 Q}{h} \frac{Z}{d^3}$	0
Tetrahedral (4)		0	0
Trigonal Bipyramidal (5)		$\frac{e^2 Q}{h} \frac{Z}{d^3}$	0
Octahedral (6)		0	0

NATURE OF M DETERMINES ^{17}O QUADRUPOLEAR COUPLING CONSTANT IN $\text{M}-^{17}\text{O}-\text{M}$ LINKAGE

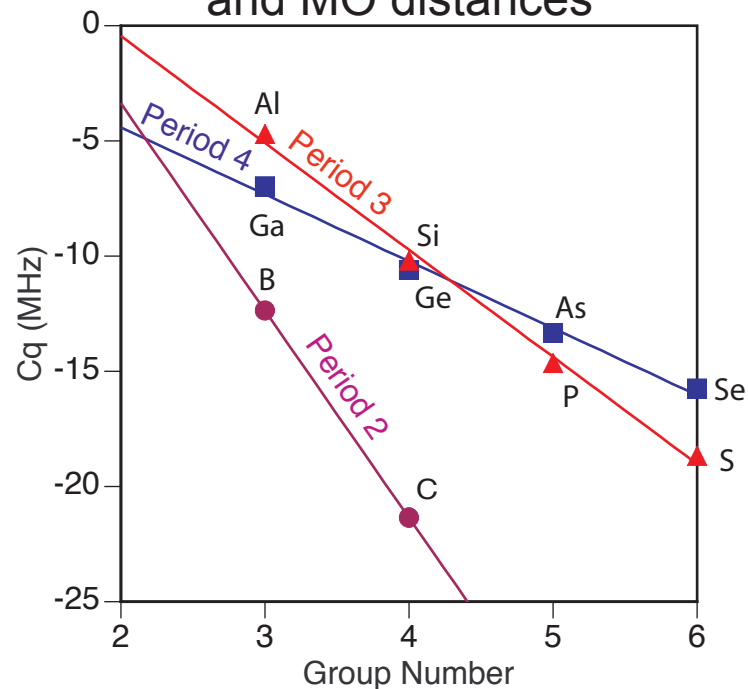


M-O-M Angle and MO distance at optimized value



AFTER OLDFIELD AND CO-WORKERS
JACS, **106**, 2502 (1984), *JACS*, **108**, 7236 (1986)
JPC, **91**, 1054 (1987).

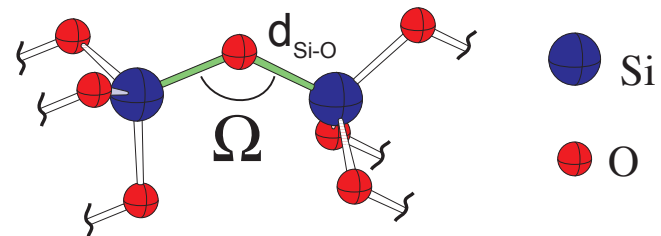
Identical M-O-M angles and MO distances



CLARK AND GRANDINETTI
SSNMR, **16**, 55 (2000).

LOCAL GEOMETRY IS SECONDARY FACTOR

HOW DOES LOCAL GEOMETRY DETERMINE BRIDGING OXYGEN EFG?



With all other factors constant ...

Bridging Oxygen $|C_q|$ values

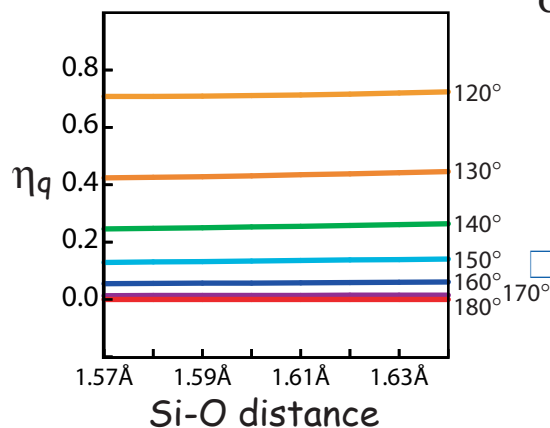
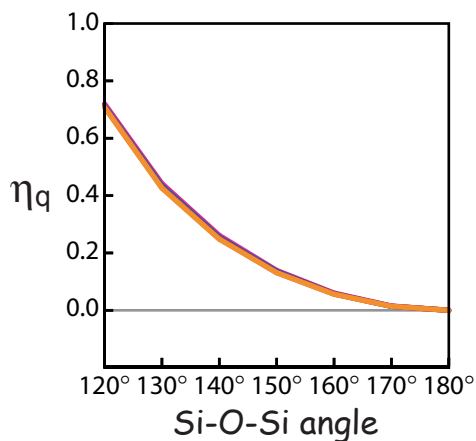
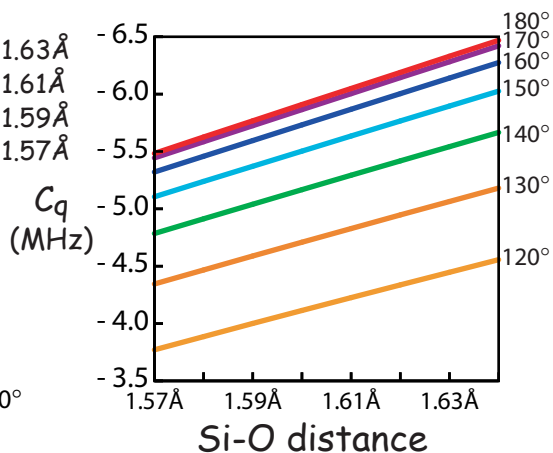
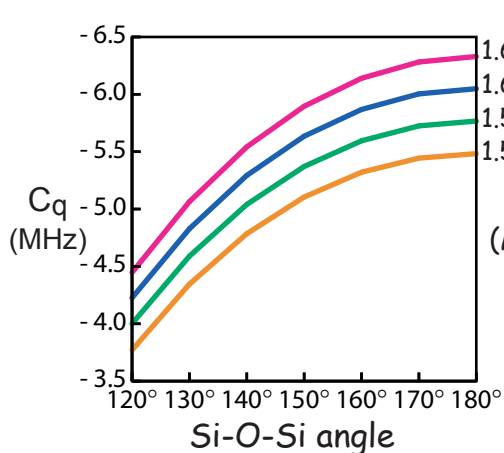
- decrease with decreasing Si-O-Si angle
- decrease linearly with decreasing Si-O distance

$$C_q(d_{\text{Si-O}}, \Omega) = -(5.91 \text{ MHz}) \left(\frac{1}{2} + \frac{\cos \Omega}{\cos \Omega - 1} \right)^{1.948} - (15 \text{ MHz/\AA}) (d_{\text{Si-O}} - 1.6 \text{ \AA})$$

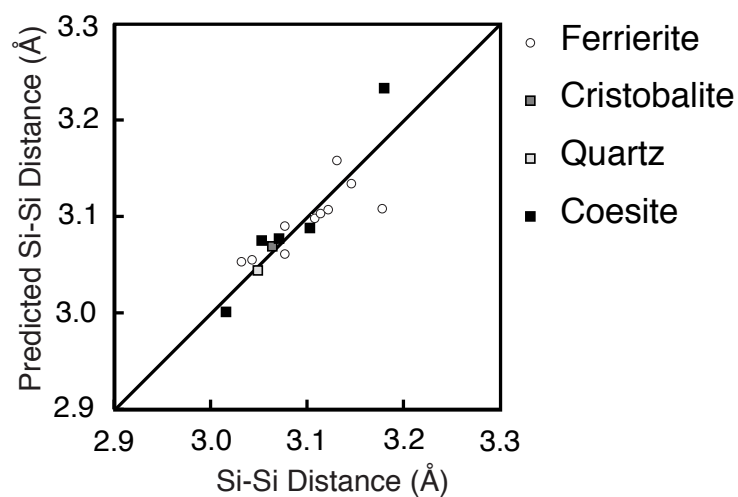
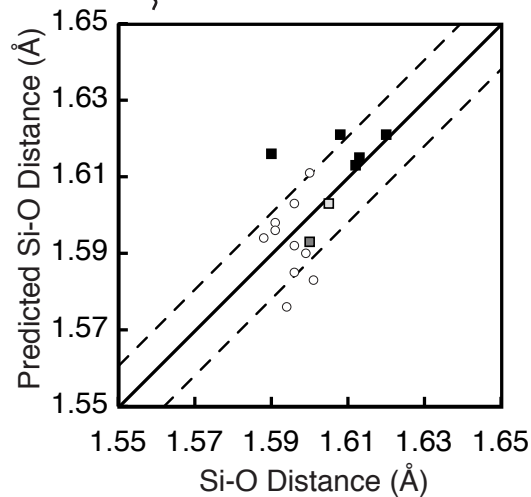
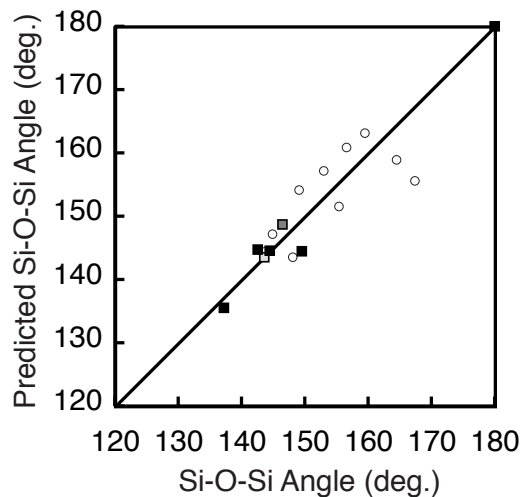
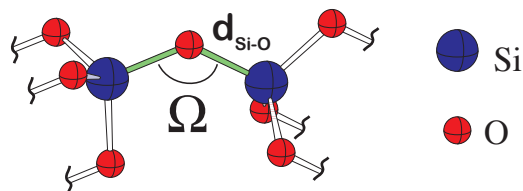
Bridging Oxygen η_q values

- increase with decreasing Si-O-Si angle
- are nearly independent of Si-O distance

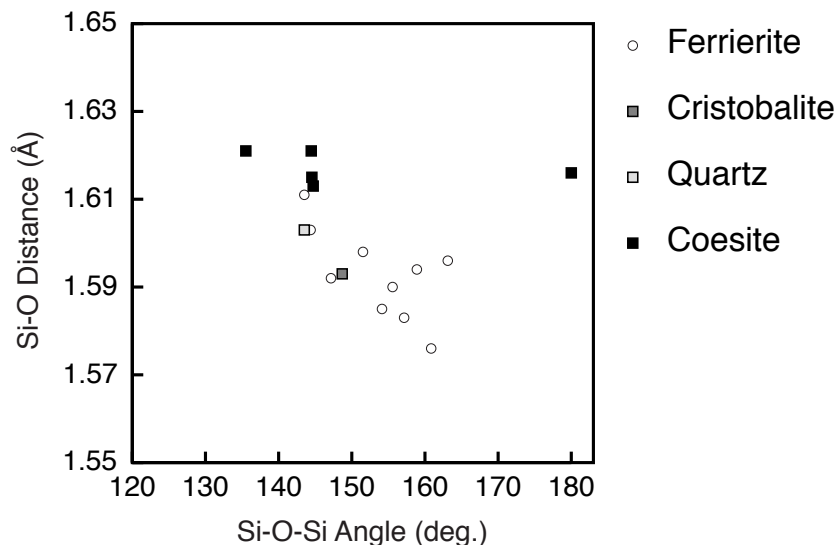
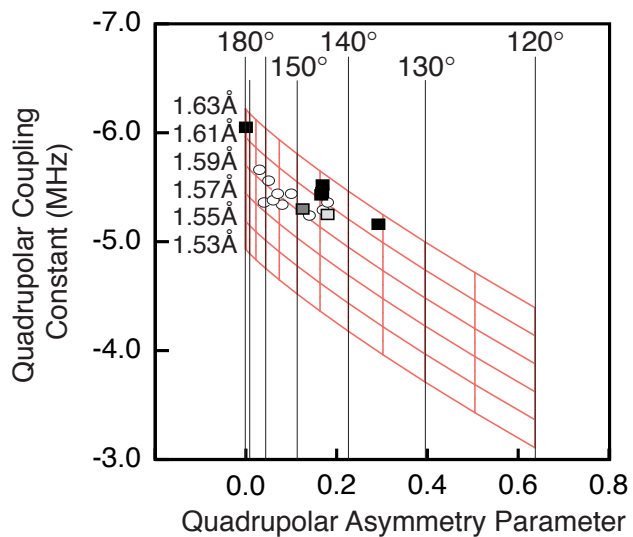
$$\eta_q(\Omega) = 5.03 \left(\frac{1}{2} - \frac{\cos \Omega}{\cos \Omega - 1} \right)^{1.09}$$



QUADROPOLAR COUPLING PARAMETERS CAN BE USED TO MEASURE ANGLES AND DISTANCES



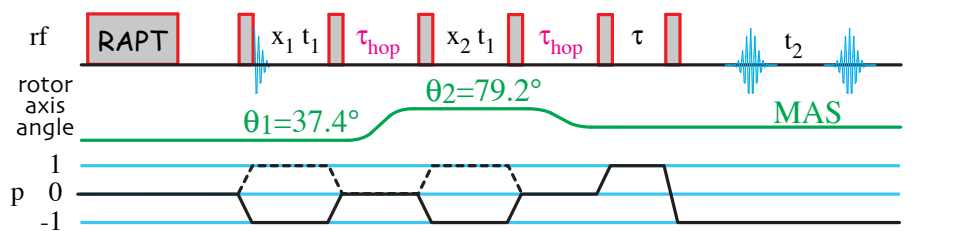
AND THEIR CORRELATIONS



RAPT ENHANCED ^{17}O DAS OF SiO_2 GLASS

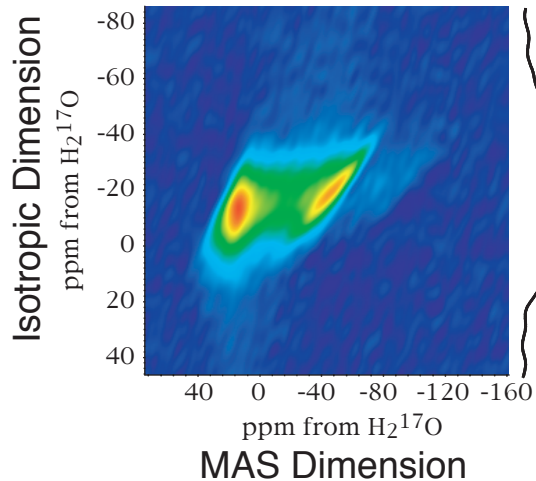
Clark, Grandinetti, Florian, Stebbins, *Phys. Rev. B*, **70**, 064202 (2004).

DISTRIBUTION AND CORRELATION OF ^{17}O NMR PARAMETERS IN SiO_2 GLASS

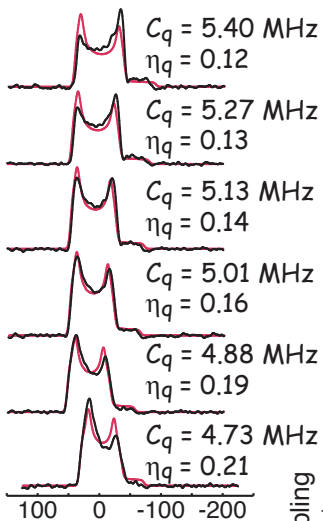


SPECTRUM TAKEN

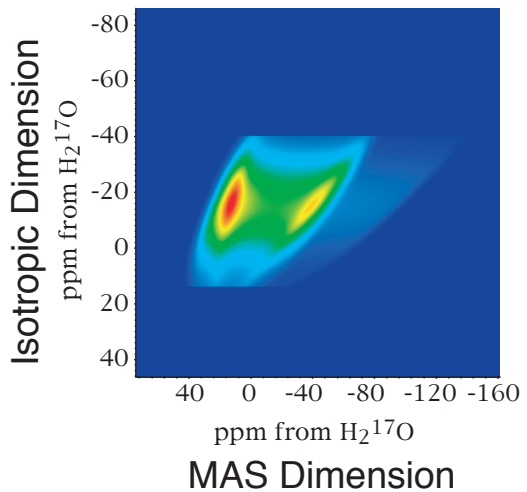
AT 9.4 TESLA



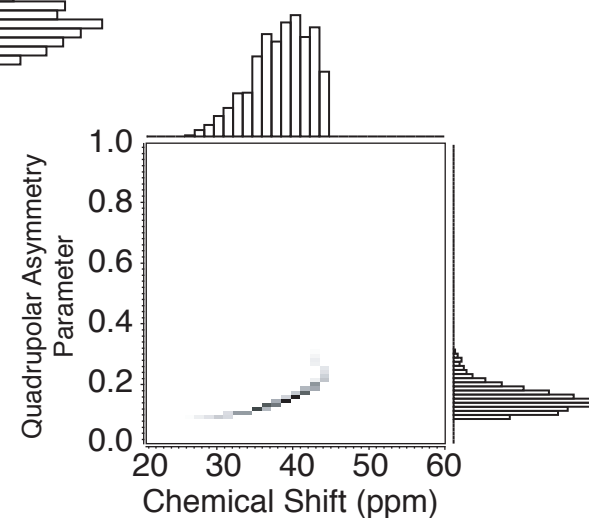
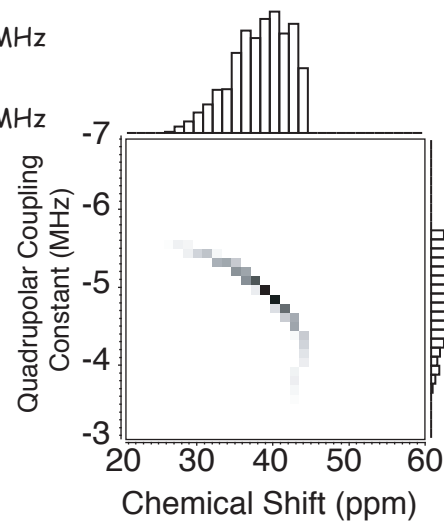
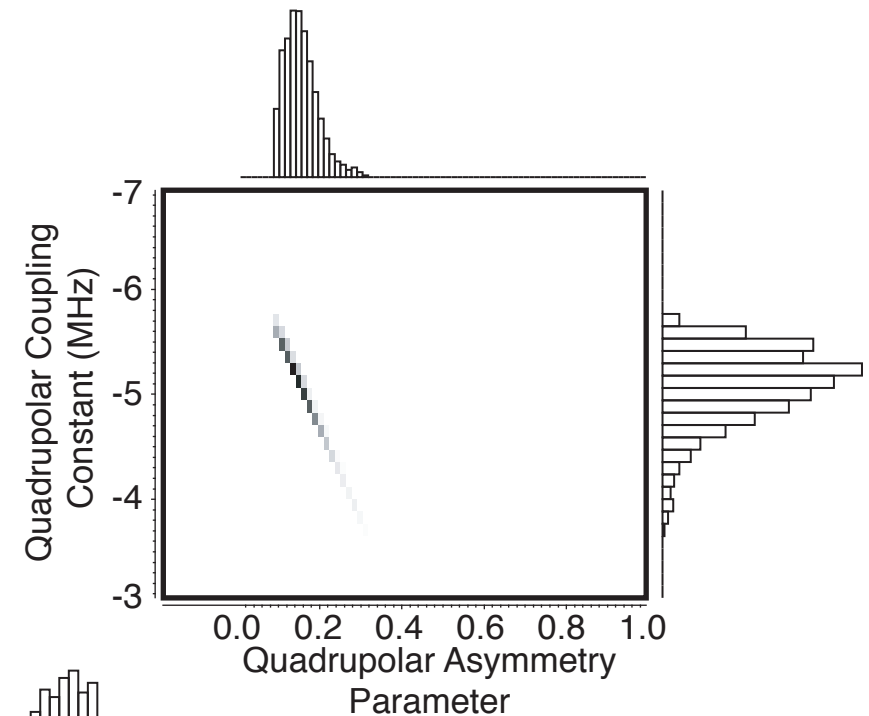
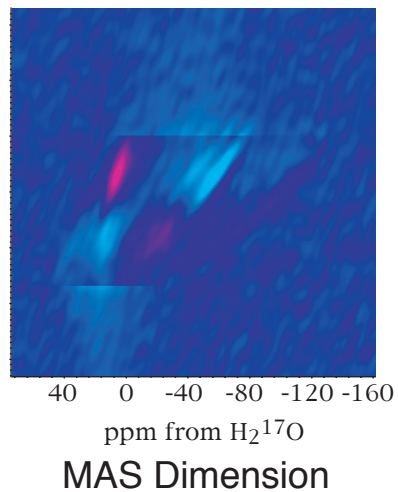
SELECTED CROSS-SECTIONS AND BEST FIT SIMULATIONS



LEAST SQUARES FIT

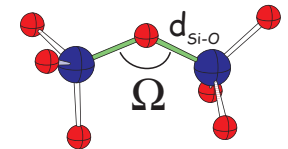
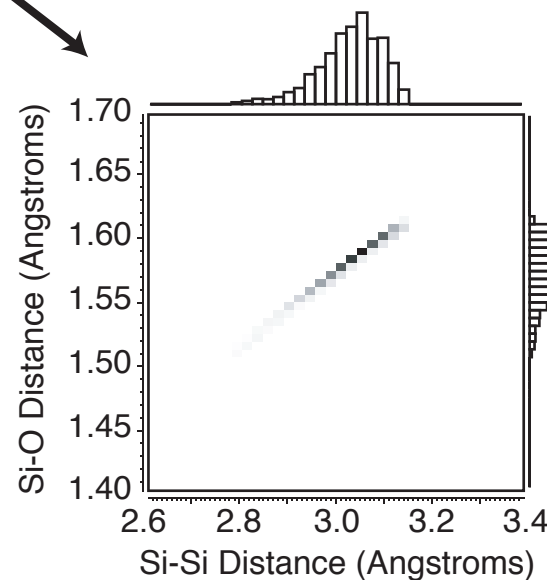
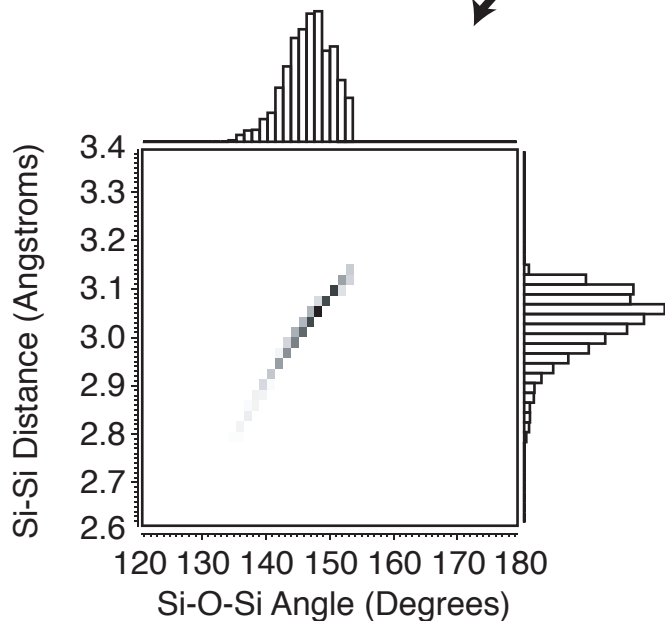
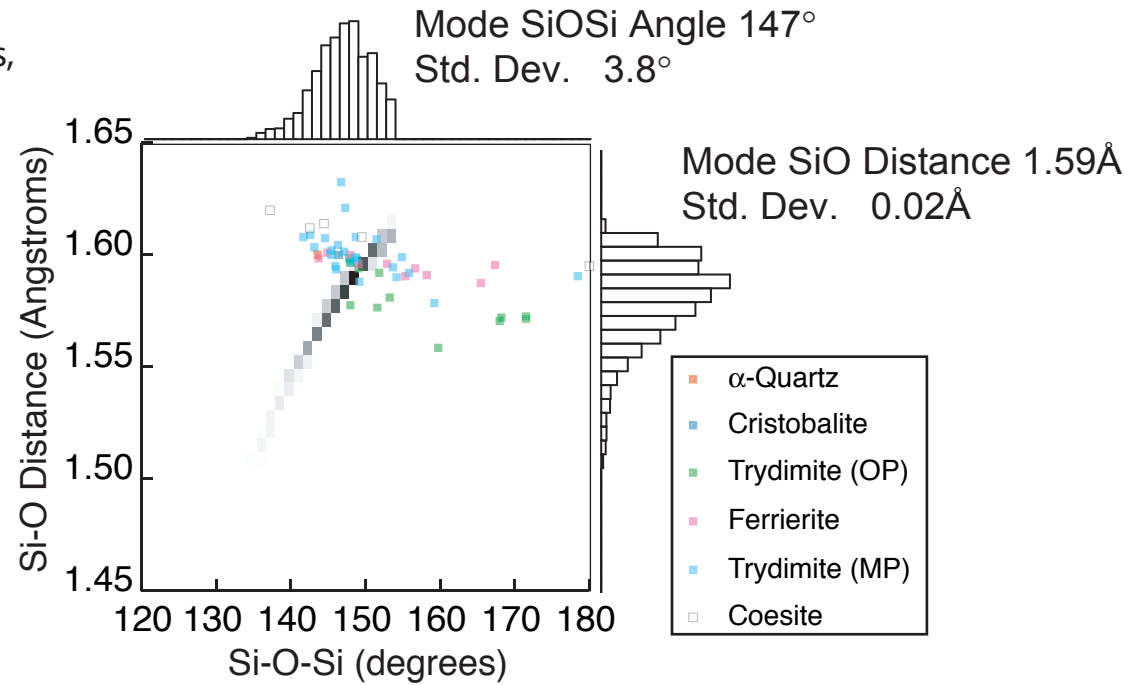
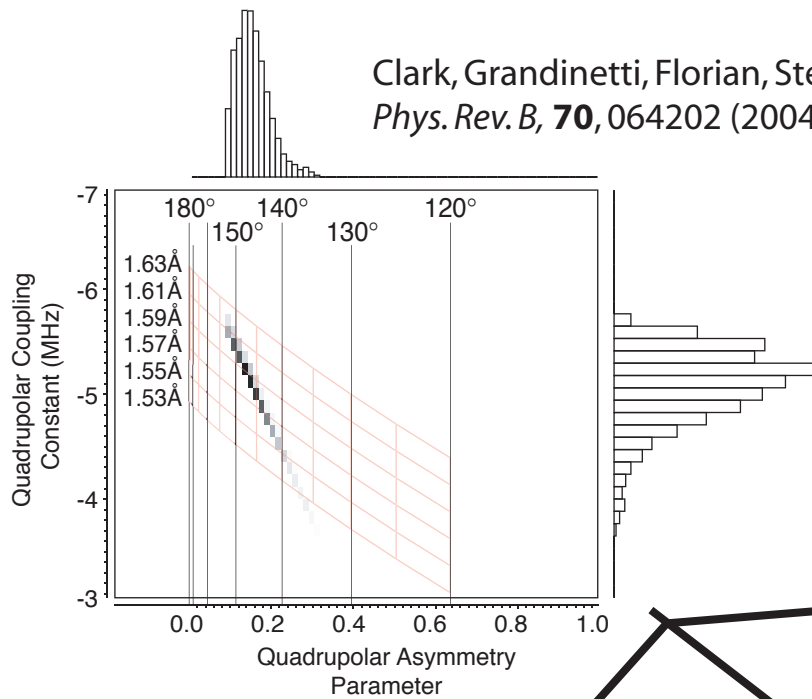


RESIDUALS



SI-O-SI ANGLE AND DISTANCE DISTRIBUTIONS IN SILICA GLASS FROM CQ AND η Q

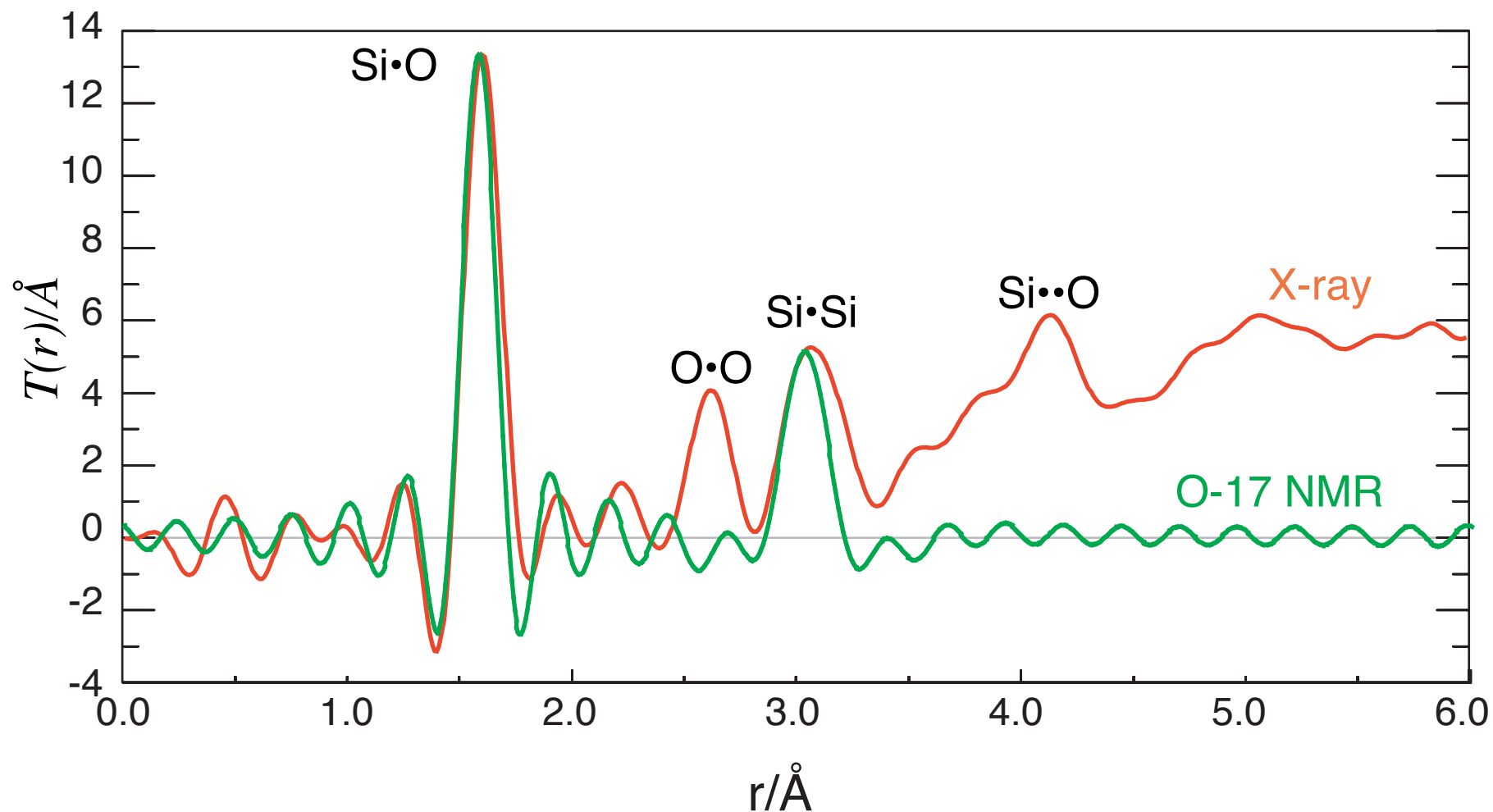
Clark, Grandinetti, Florian, Stebbins,
Phys. Rev. B, **70**, 064202 (2004).



In Silica Glass
Si-O distance decreases
as Si-O-Si angle decreases !!

Mode Si- Si Distance 3.04 Å
Std. Dev. 0.06 Å

COMPARISON OF MODIFIED NMR DISTANCE DISTRIBUTIONS WITH X-RAY



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